

- 2nd Talk: Phenotypic Evolution
- **Evolutionary Fluctuation-Response Relation**
- **Evolution of Robustness, Genotype-Phenotype Relation**
- Sympatric Speciation as a result of phenotype differentiation
- Evolution of Development
- Spontaneous Adaptation by Noise
- Summary+Discussion

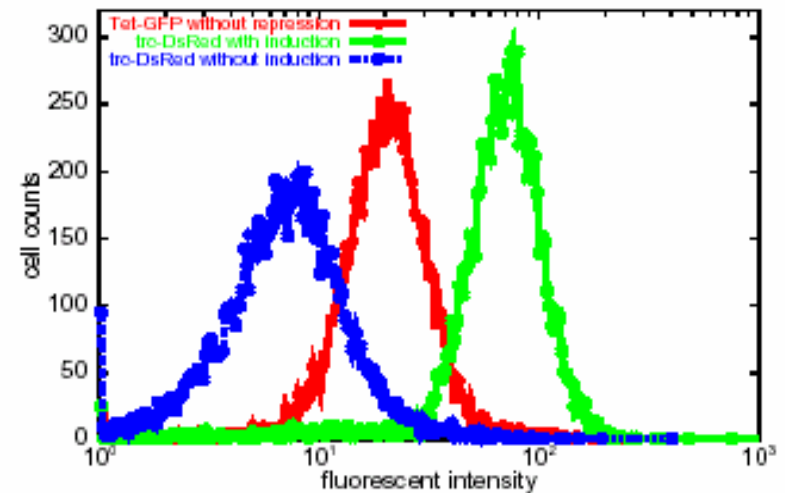
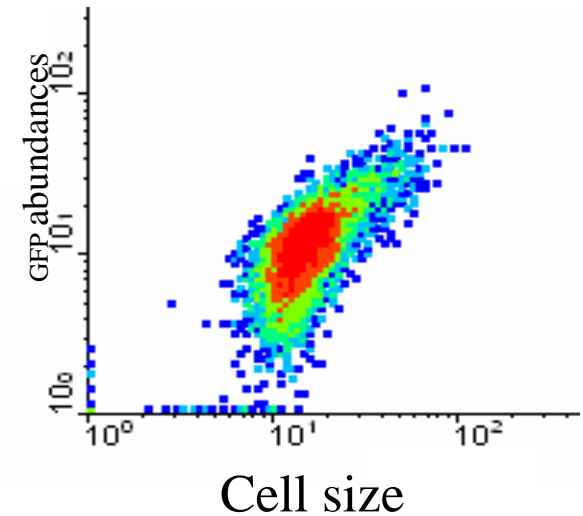
Motivation 1: Phenotypic Fluctuation → evolution ?

- Even in isogenic individuals (clones) there is large phenotypic fluctuation

Recognized now extensively

Exp + Model+Theory

- Relevance of this fluctuation to evolution?
- Positive role of noise?



number distribution of the proteins measured by fluorescent intensity.

three *Escherichia coli* cell populations containing different reporter plasmids.

• Phenotypic Fluctuation → Relationship to Evolution?

* **Standard evolutionary genetics;**

(0) selection is based on phenotype

(activity, size, protein abundances, fluorescence,...),

$\text{Fitness}(\text{phenotype})$

(i) gene $a \rightarrow$ phenotype x

→ if this mapping is uniquely determined

→ $\text{Fitness}(\text{Genotype})$ instead

(ii) only genotype is transferred the offspring

Change of distribution $P(\text{genotype}) \rightarrow$ evolution

But gene—“development” \rightarrow Phenotype

Is not necessarily unique

Phenotypic fluctuation of isogenic organisms

→ $P(x; a)$ x —phenotype, a – gene

Motivation2: Evolution of Robustness

- Robustness ----- Insensitivity of Fitness (Phenotype) to system's change
 - ← due to environmental change
 - ← against noise during 'developmental process
 - ← against parameter change by mutation

*Question :

relationship among these robustness
condition for evolution of robustness

Background

- (1) relationship between development and evolution,
- (2) robustness increases through evolution? ---

Schmalhausen's stabilizing selection: Waddington's canalization

- (3) Landscape in Geno-pheno coupling (,Ancel-Fontana.Wagner,..)

Motivation 1 and 2, combined:

- (A) Plasticity, Potency, Flexibility, (Robustness), Evolvability Traditional concepts

Ambiguous Concepts; Often Explained only Verbally but probably important biologically (as an organism level)

- * (B) Quantitative Biological studies on dynamics and fluctuations: Progresses rapidly recently
- Still Large Gap between (A) and (B);
- Especially when (A) concerns with macroscopic biological characteristics

Need to fill the gap

(cf: stat mechanics is constructed after establishment of thermodynamics to be consistent)

Plasticity Measure

--- changeability (response against external change)

--- related with
degree of fluctuation ?
(negatively correlated with) robustness

So-called fluctuation-dissipation theorem in physics:

Force to change a variable x ;

response ratio = (shift of x) / force

fluctuation of x (without force)

response ratio proportional to **fluctuation**

originated by Einstein's paper a century ago...

Generalization::(mathematical formulation)

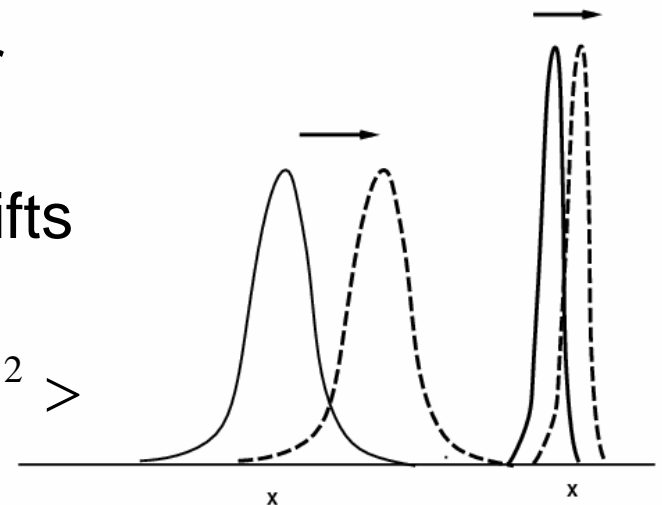
response ratio of some variable x against the change of parameter a versus **fluctuation of x**

$P(x;a)$ x variable, a : control parameter

change of the parameter $a \rightarrow$

peak of $P(x;a)$ (i.e., $\langle x \rangle$ average) shifts

$$\frac{\langle x \rangle_{a+\Delta a} - \langle x \rangle_a}{\Delta a} \propto \langle (\delta x)^2 \rangle_a = \langle (x - \langle x \rangle)^2 \rangle$$



Fluctuation-response relationship (generalized form)

Gaussian distribution of x ; under the parameter a

$$P(x; a_0) = N_0 \exp\left(-\frac{(x - X_0)^2}{2\alpha_0}\right), \quad \text{at } a=a_0$$

Change the parameter from a_0 to a

$$P(x : a) = N \exp\left(-\frac{(x - X_0)^2}{2\alpha(a)} + v(x, a)\right)$$

$$v(a, x) = C(a - a_0)(x - X_0) + \dots, \text{ with } C \text{ as a constant,}$$

$$P(x : a) = N(a) \exp\left(-\frac{(x - X_0)^2}{2\alpha(a)} + C(a - a_0)(x - X_0)\right),$$

generalized force $C(a - a_0)(x - X_0)$ to shift the distribution.

$$P(x, a_0 + \Delta a) = N' \exp\left(-\frac{(x - X_0 - C\Delta a\alpha(a_0 + \Delta a))^2}{2\alpha(a_0 + \Delta a)}\right)$$

Hence, we get

$$\frac{\langle x \rangle_{a=a_0+\Delta a} - \langle x \rangle_{a=a_0}}{\Delta a} = C\alpha(a_0 + \Delta a),$$

Noting that $\alpha = \langle (\delta x)^2 \rangle$

$$\frac{\langle x \rangle_{a=a_0+\Delta a} - \langle x \rangle_{a=a_0}}{\Delta a} = C \langle (\delta x)^2 \rangle,$$

Approximate formula ; trivial by itself

Non-trivial point : representation by $P(x;a)$

x : phenotype **a** ; enviroment etc

- General Viewpoint:

x: phenotype (variable)

a: genotype (parameter)

parameter \rightarrow variable: condition (1)

a: scalar continuous parameter showing
gene (say, number of matched sequences etc.)

for given direction of specific function,

x is distributed even if gene (a) is specified

consider $P(x;a)$ under given environment h

Environment h change to select 'a' value

selection \rightarrow change in $P(x;a)$

Artificial selection experiment with bacteria
for enzyme with higher catalytic activity
for some protein with higher function

Change in gene (parameter; a) \Rightarrow

“Response” ----- change of phenotype $\langle x \rangle$

(e.g., fluorescence intensity)

per generation per (synonymous) mutation rate

Fluctuation ---- Variance of phenotype x of clone

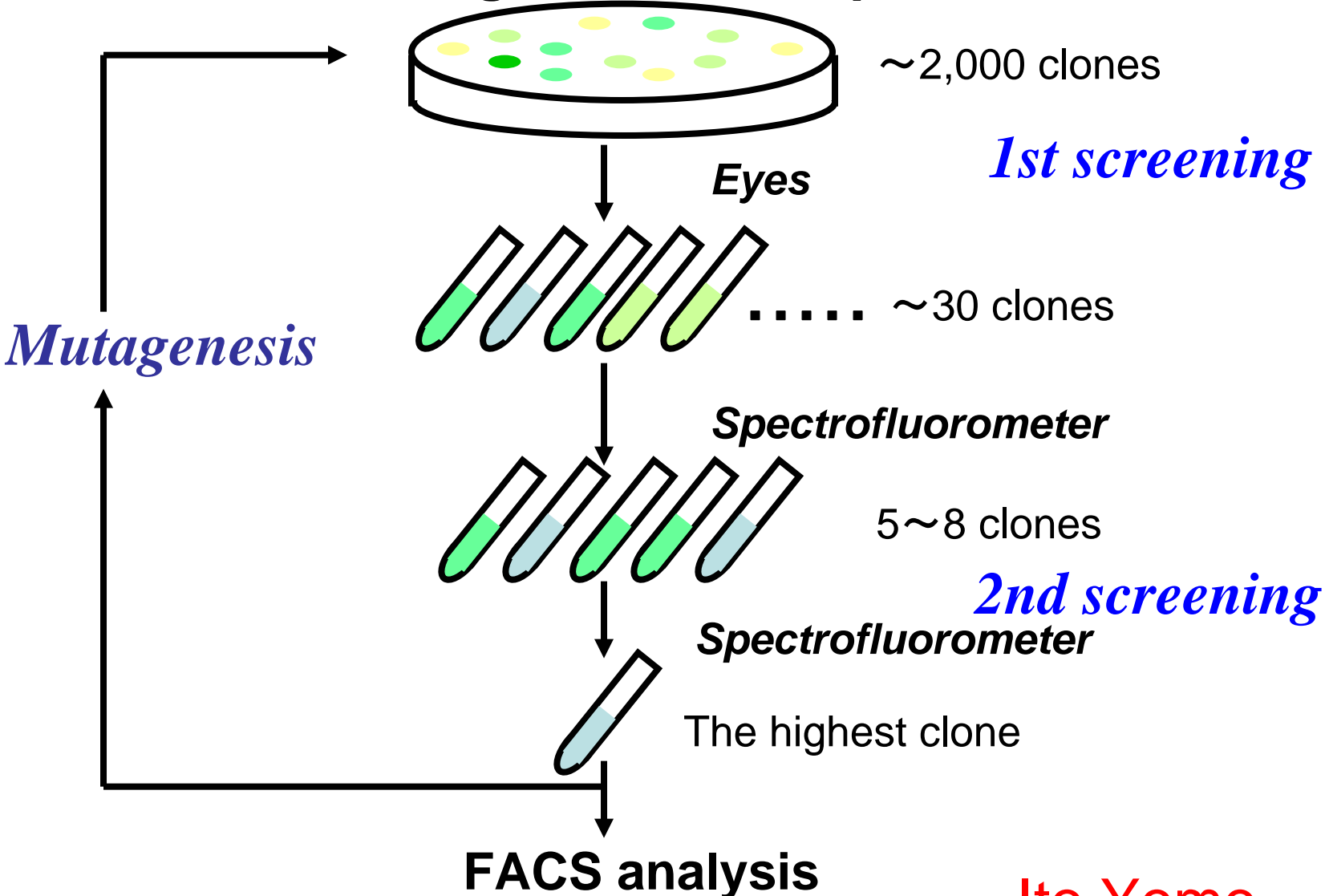
Fluctuation in the phenotype x of clone

\Leftrightarrow speed of evolution to increase $\langle x \rangle$

(proportional or correlated)

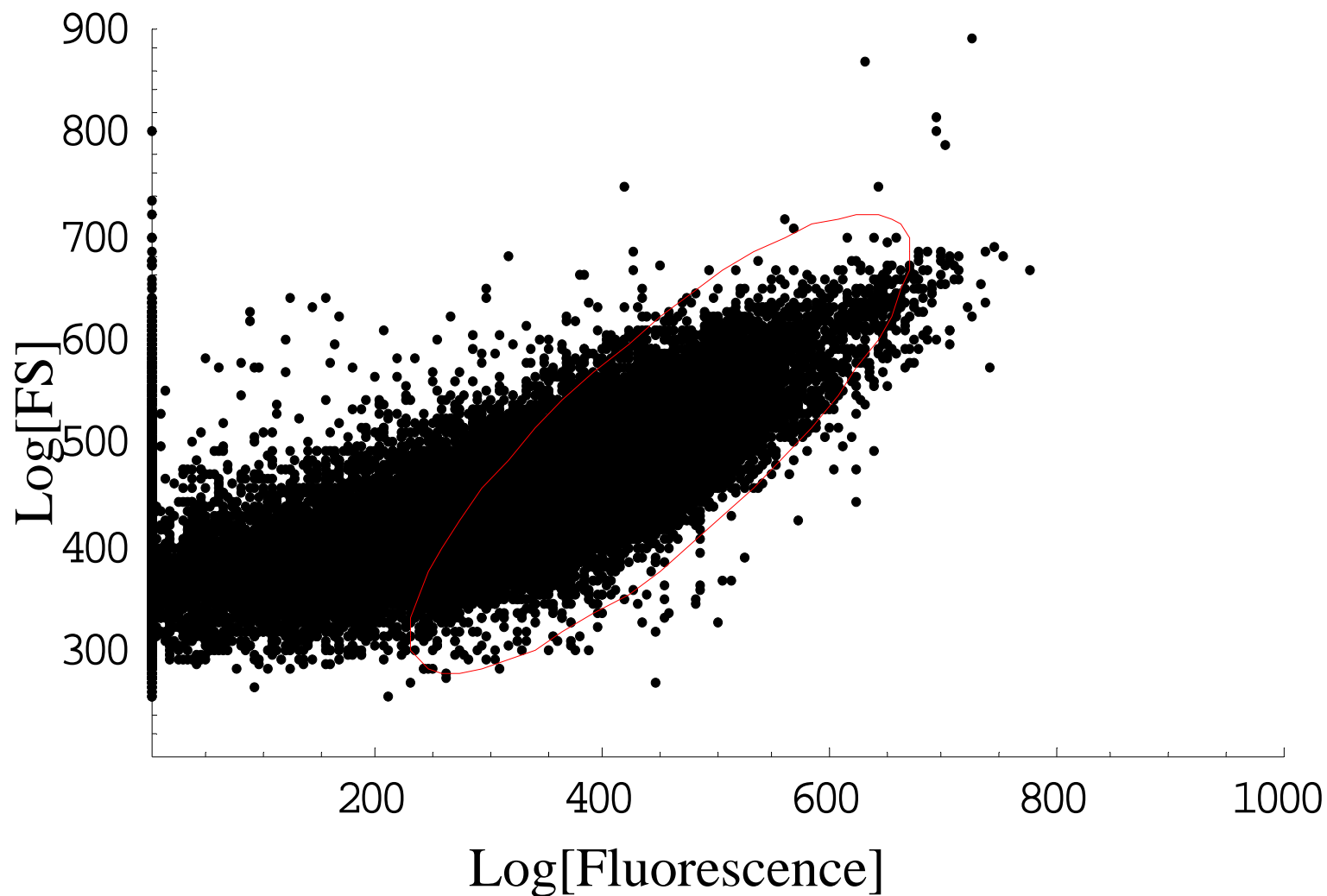
Artificial selection experiment with bacteria
Selection to increase the fluorescence of protein in bacteria

Schematic drawing of selection process

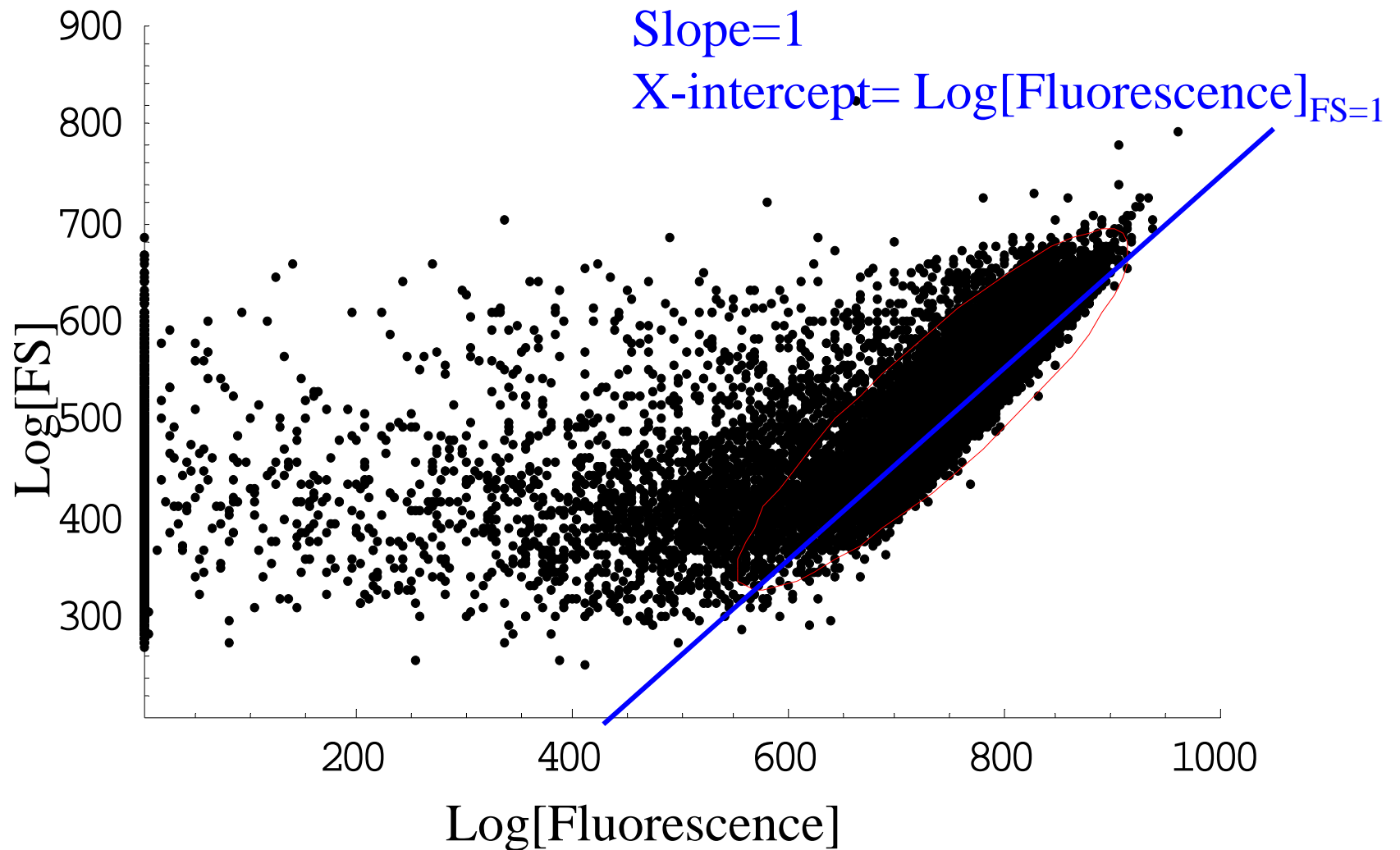


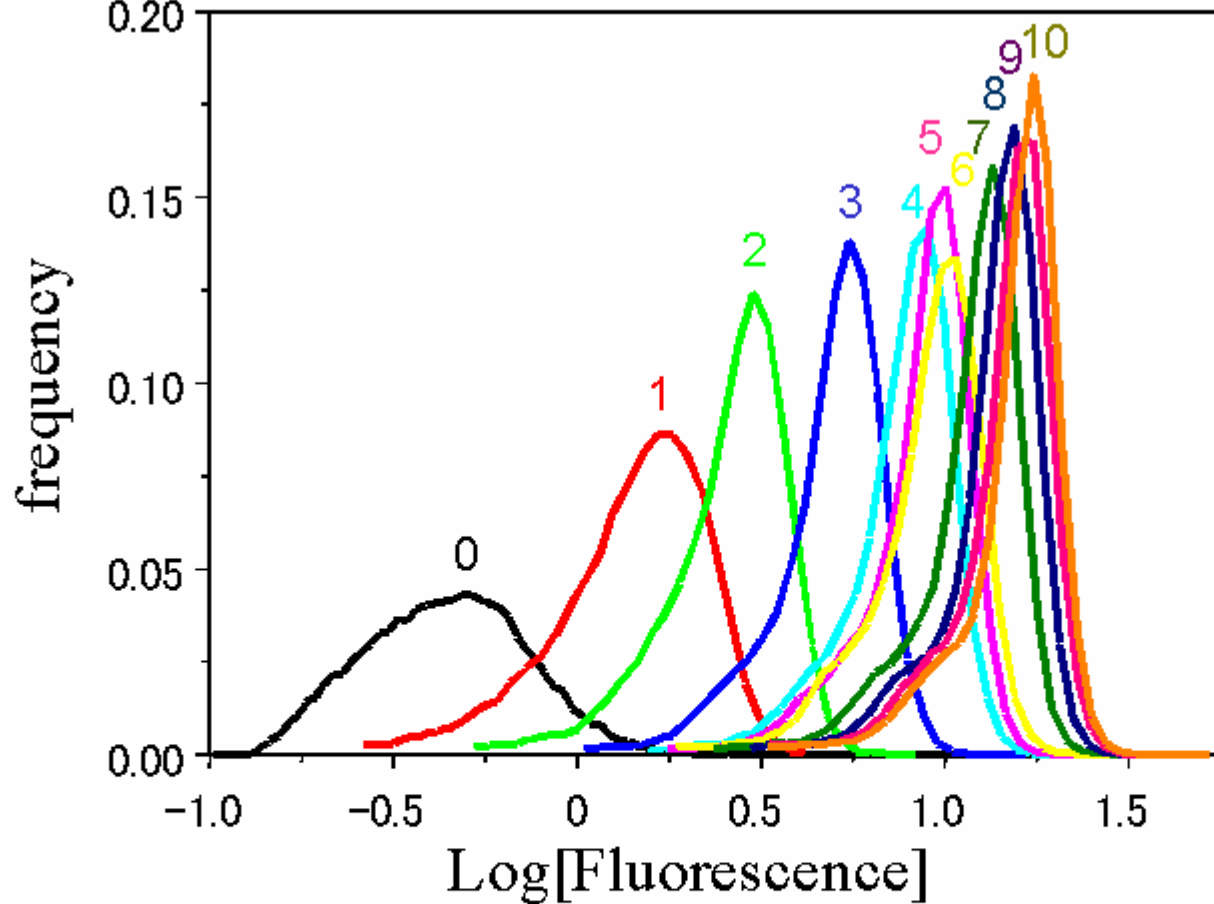
Ito, Yomo,...

RP-334Log.LMD



I10-6Log.LMD





Sato, Ito,
Yomo, KK
PNAS(2003)

Fluctuation --- Variance of phenotype of clone

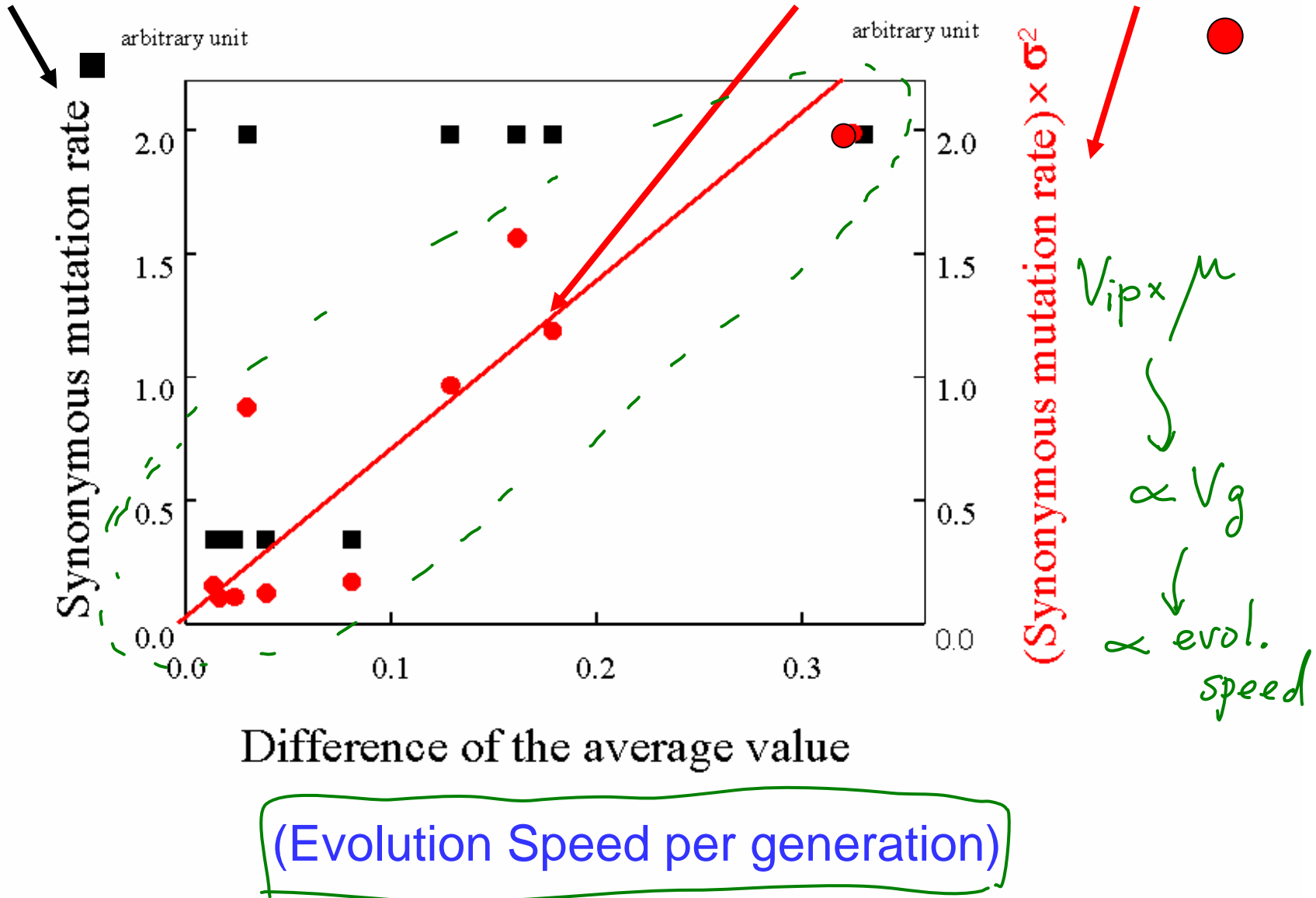
Organisms with larger phenotypic fluctuation higher evolution speed;

- change of phenotype per generation per mutation --
``Response against mutation+selection''

Response \leftrightarrow Fluctuation

Naïve expectation:
Just prop to mutation rate

Fluctuation-response relation
Phenotype fluct. \times mutation rate



Cofirmation by model:

Toy Cell Model with Catalytic Reaction Network

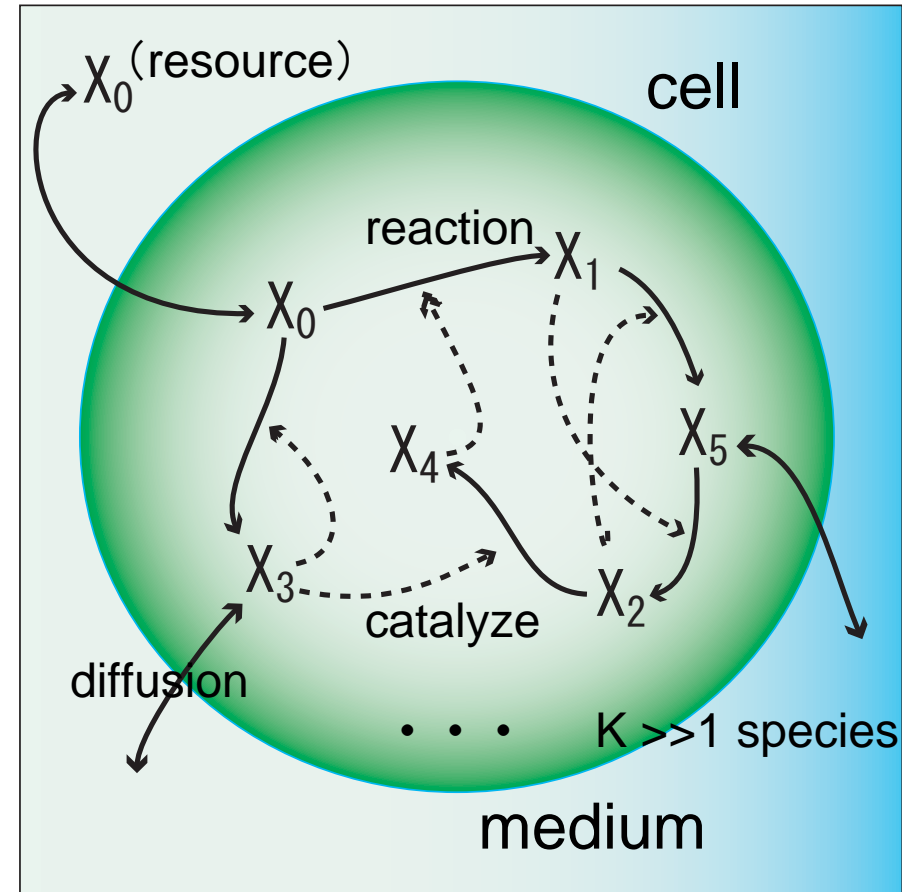
C. 細胞 Furusawa & KK

■ **k species of chemicals** 、 $X_0 \cdots X_{k-1}$
number --- $n_0, n_1 \dots n_{k-1}$

■ **random catalytic reaction network**
with the path rate p
for the reaction $X_i + X_j \rightarrow X_k + X_j$

■ some chemicals are **penetrable**
through the membrane with the
diffusion coefficient D

■ resource chemicals are thus
transformed into impenetrable
chemicals, leading to the growth in
 $N = \sum n_i$ when it exceeds N_{\max}
the cell divides into two



model

- Confirmation by numerical evolution experiment by the reaction-net cell model

Mutate the network ('gene') with mutation rate μ , (rewire the path of the network with the rate) and select such network having highest concentration c of a specific chemical

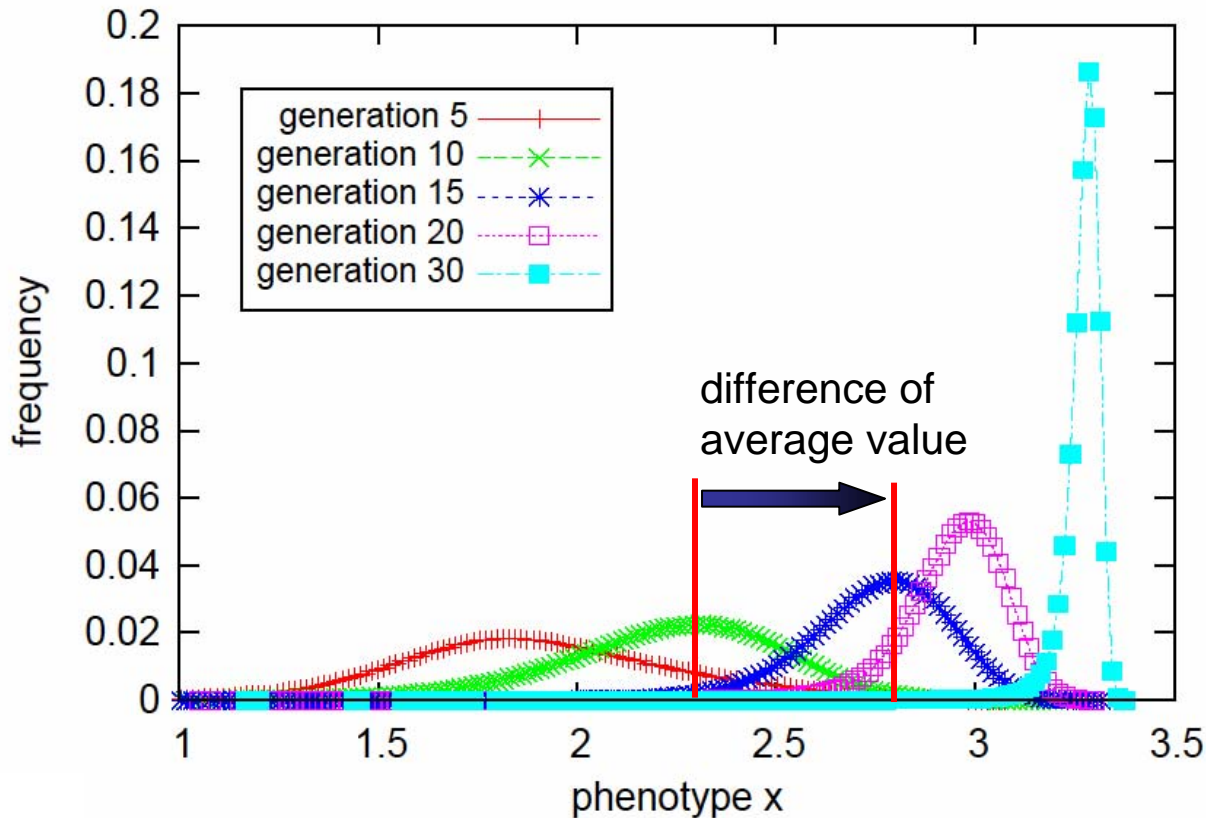


1. Prepare initial mother cells.
2. From each parent cell, mutant cells are generated by randomly replacing reaction paths, with **mutation rate μ**
3. reaction dynamics of all mutants are simulated to determine phenotype x
4. Top 5% cells with regard to phenotype x are selected as parent cells of next generation

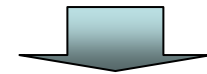
phenotype $x = \log(n_s)$

Fluctuation of Phenotype x

Change of distribution of phenotype x through evolution

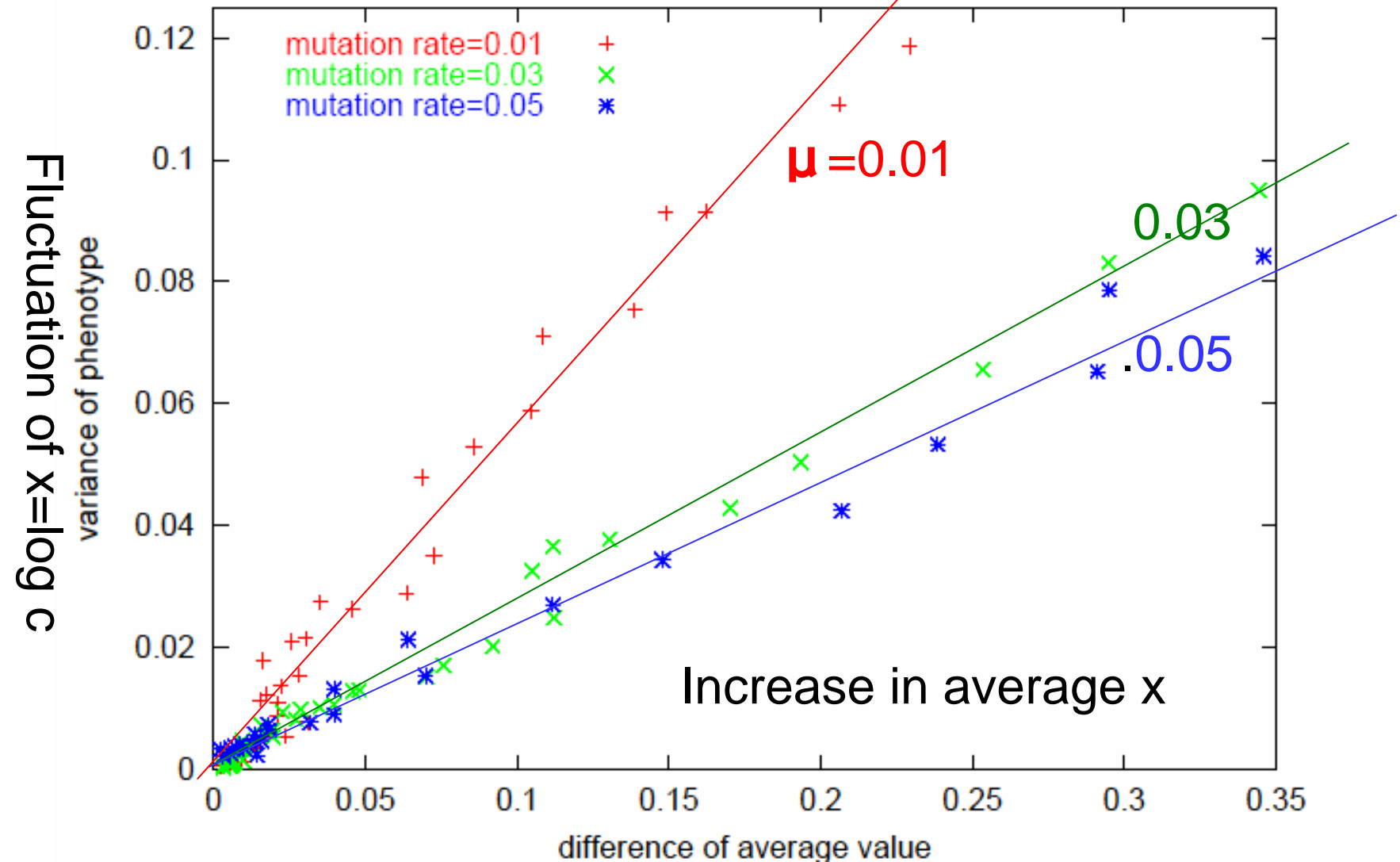


Prepare 10^5 clonal cells
(having an identical network)



Distributions of phenotype x
are plotted.

Confirmation of Fluctuation Dissipation Theorem by reaction-network cell model



(1) the use of $\log(\text{fluorescence})$, because $\log x$ is close to Gaussian distribution in experiments

(2) New mystery? **phenotype fluctuation of clone vs evolution speed** in contrast to evolution speed \propto phenotypic fluctuation by genetic variation (V_g): (fundamental theorem of natural selection; established)

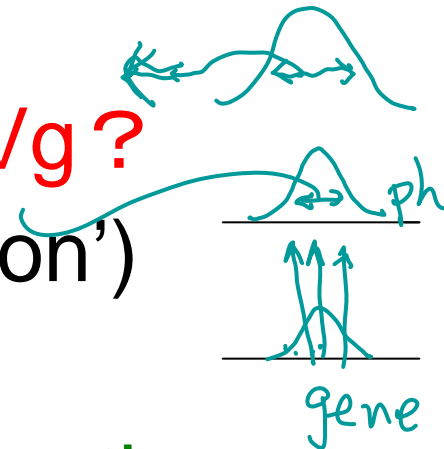
pheno fluct of clone V_p

\propto **pheno fluct by gene variation V_g ?**

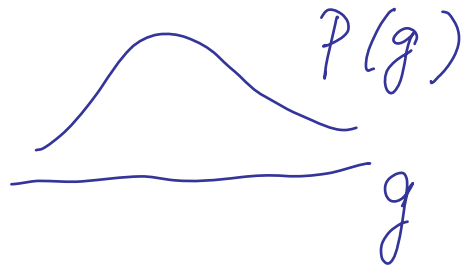
(fluct by noise \propto variation in 'equation')

Follow the spirit of Einstein;

micro-macro consistency \rightarrow Brownian motion



$V_{ip} \propto$ evolution speed (exp (?), model)
 $V_g \propto$ evolution speed (Fisher) a simple derivation(?)



distribution

$P_n(g)$

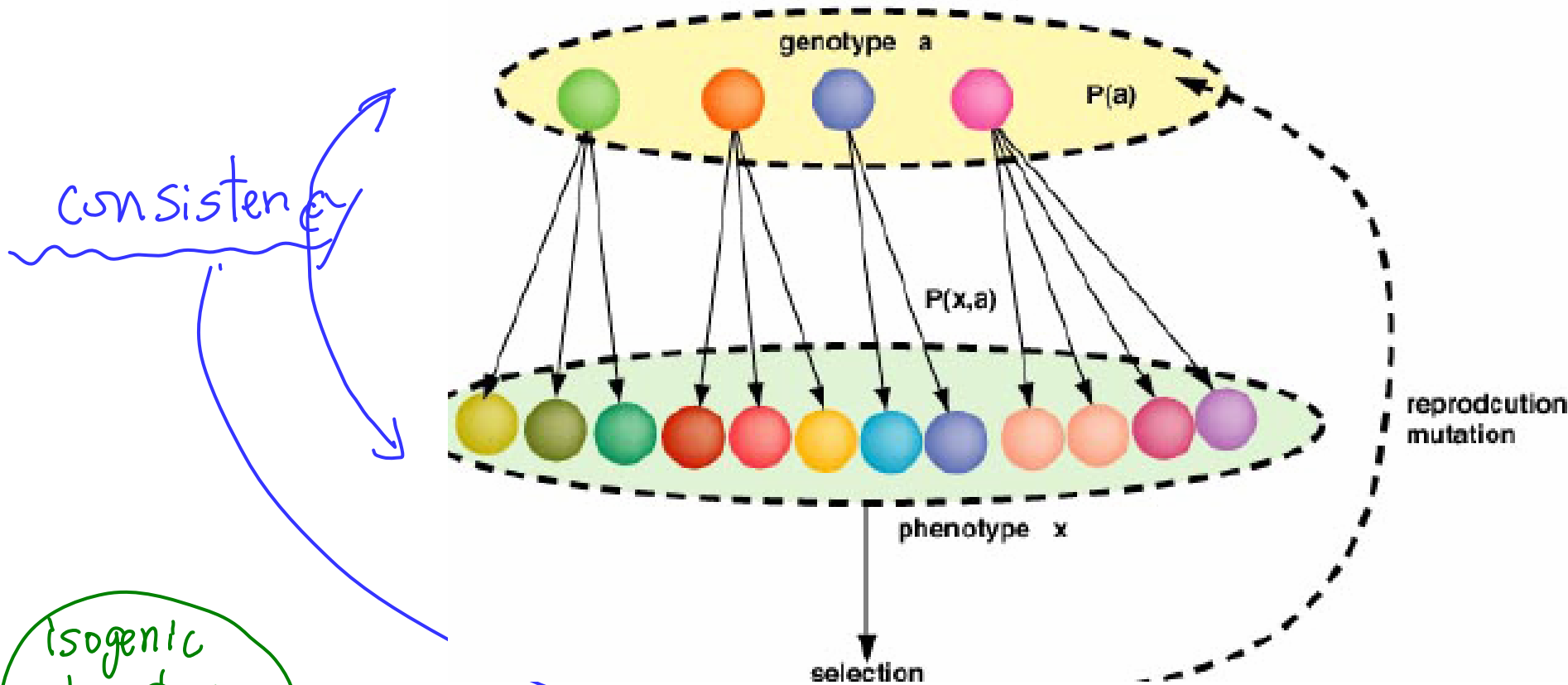
(growth rate
 \sim fitness)

$$\bar{g}_n = \int g P_n(g) dg$$

$$P_{n+1}(g) = \frac{g P_n(g)}{\int g P_n(g) dg} = \frac{g P_n(g)}{\bar{g}_n}$$

$$\begin{aligned} \bar{g}_{n+1} - \bar{g}_n &= \frac{\int g^2 P_n(g) dg}{\bar{g}_n} - \bar{g}_n = \frac{1}{\bar{g}_n} \left(\int g^2 P_n(g) dg - (\int g P_n(g) dg)^2 \right) \\ &= \frac{1}{\bar{g}_n} \overline{(g - \bar{g}_n)^2} \end{aligned}$$

(Fisher ?)



isogenic phenotypic fluct.

genotype (a)
(same)

genotype (distributed)

evolution speed

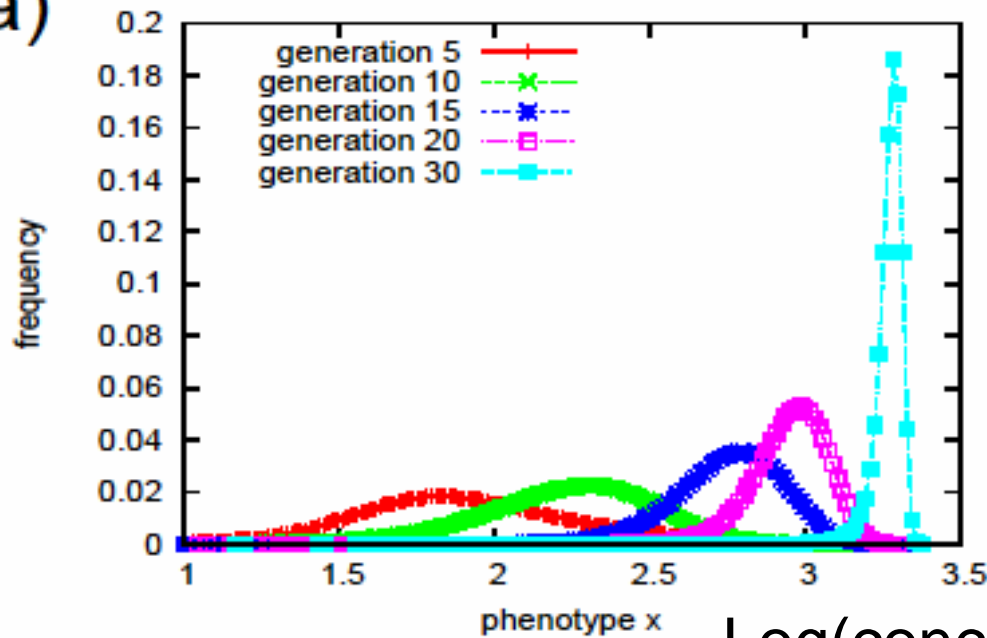


phenotype x



? V_{ip} ??

(a)

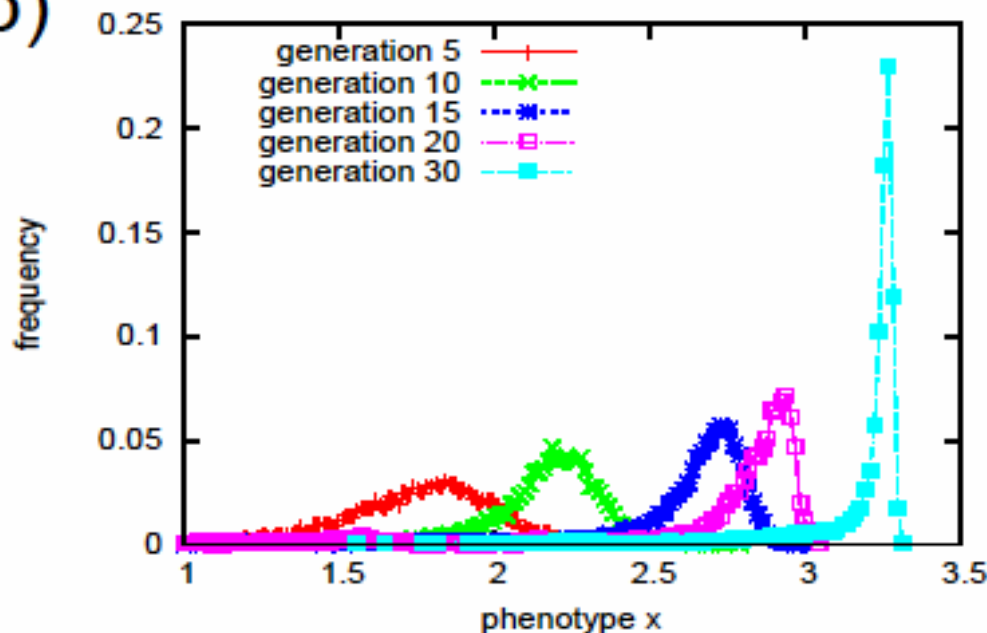


Change of distribution
through evolution

Distribution of phenotype
 x of a clone
 $\rightarrow V_p$

Log(concentration)

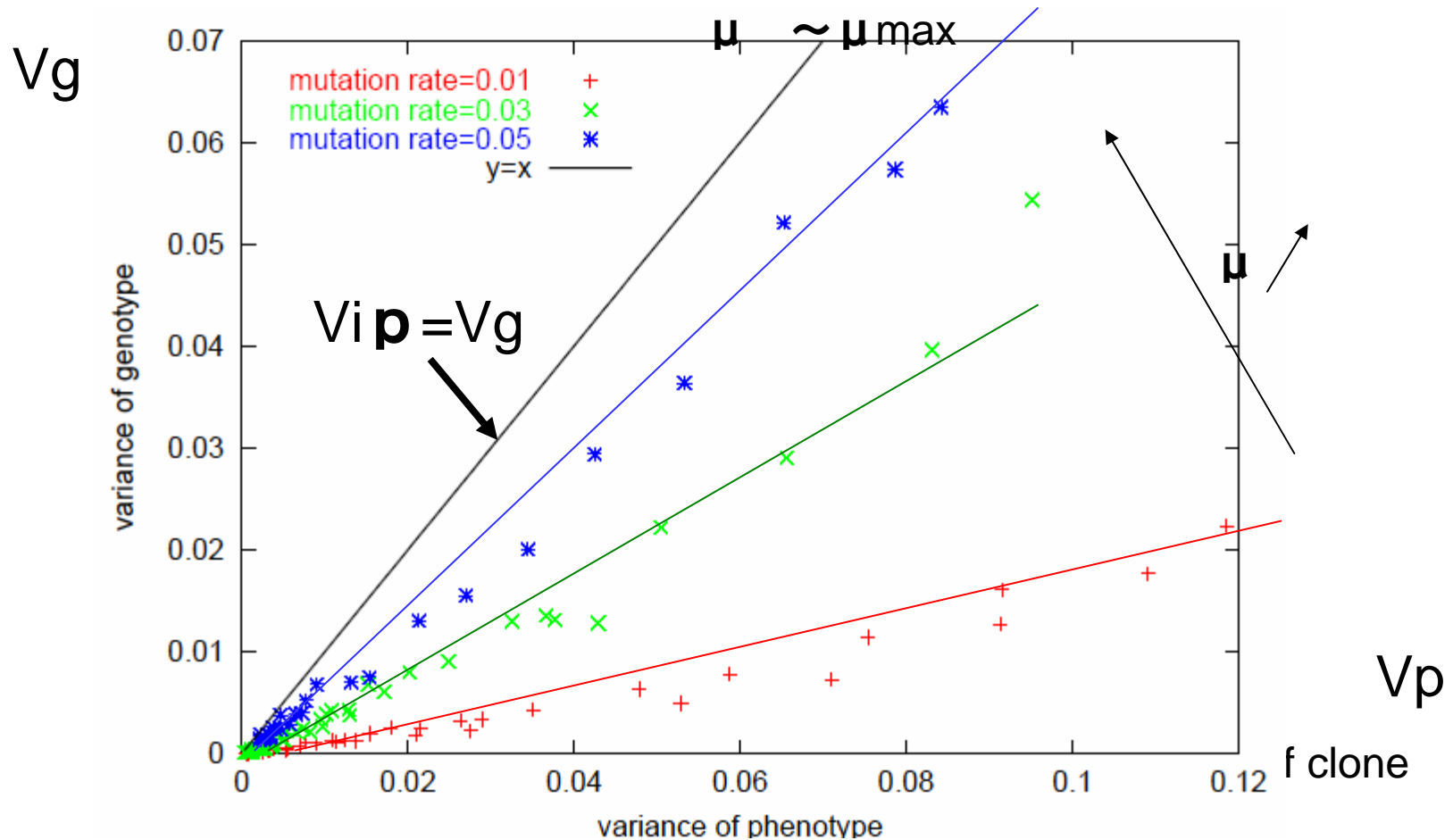
(b)



Distribution of phenotype
 x over mutants (genetic
variation)
 $\rightarrow V_g$

Phenotype fluct. (V_p) vs Gene Fluct. (V_g) in the evolution of toy cell model

V_p : fluct. for given network, V_g : fluct. by network variation



variance of $\log(x)$,
x is the concentration of the molecule

Beyond Darwin with the spirit of Einstein!

As μ (mutation rate) increases to μ_{\max} ,

(1) the distribution collapses (error catastrophe)

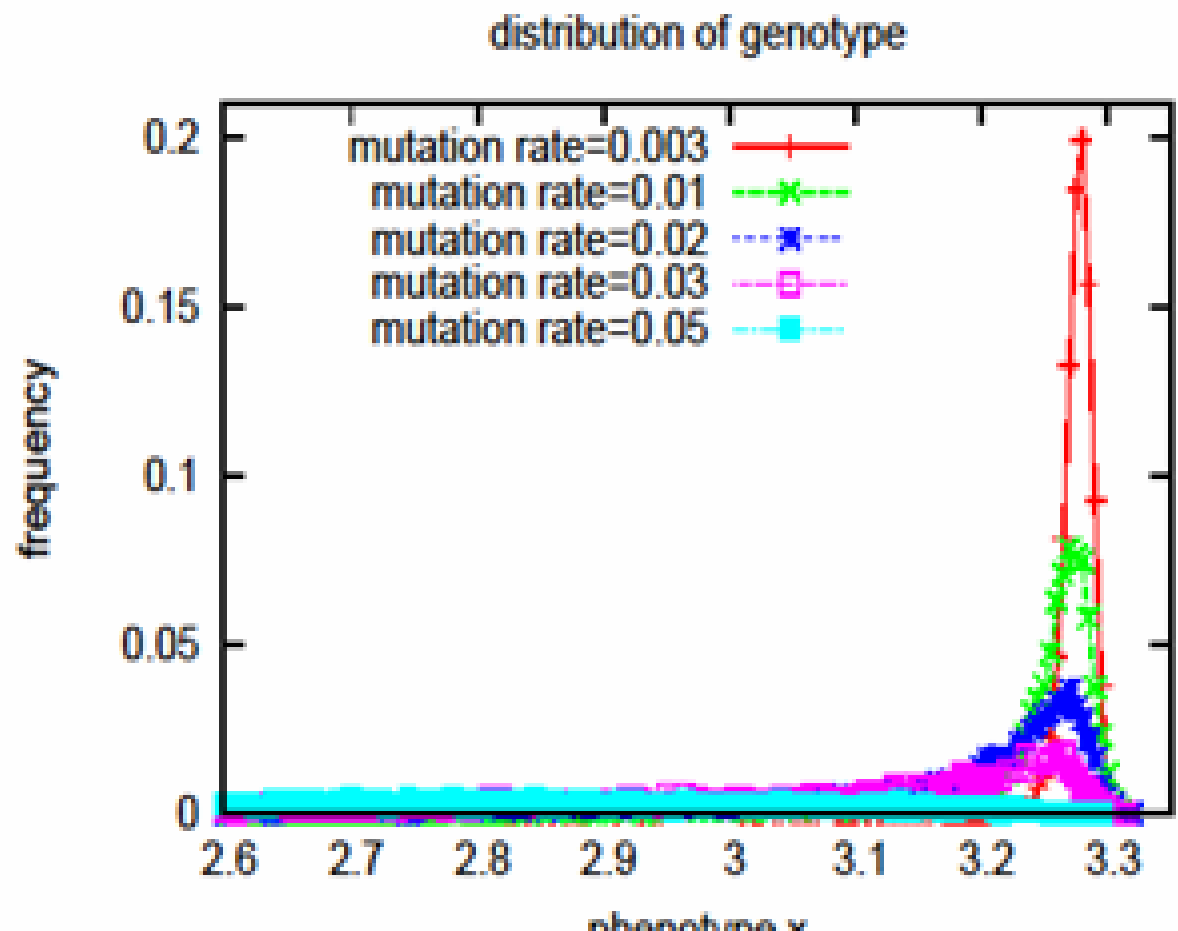
(2) evolution no longer progresses beyond μ_{\max}

evolution speed is maximal at $\mu \sim \mu_{\max}$

(3) V_g approaches V_p

As μ is increased,
The distribution
'collapses'

Error catastrophe



Consider 2-variable distrib

$$P(x=\text{phenotype}, a=\text{genotype}) = \exp(-V(x, a))$$

Keep a single-peak (stability condition).

KK, Furusawa, 2006 JTB

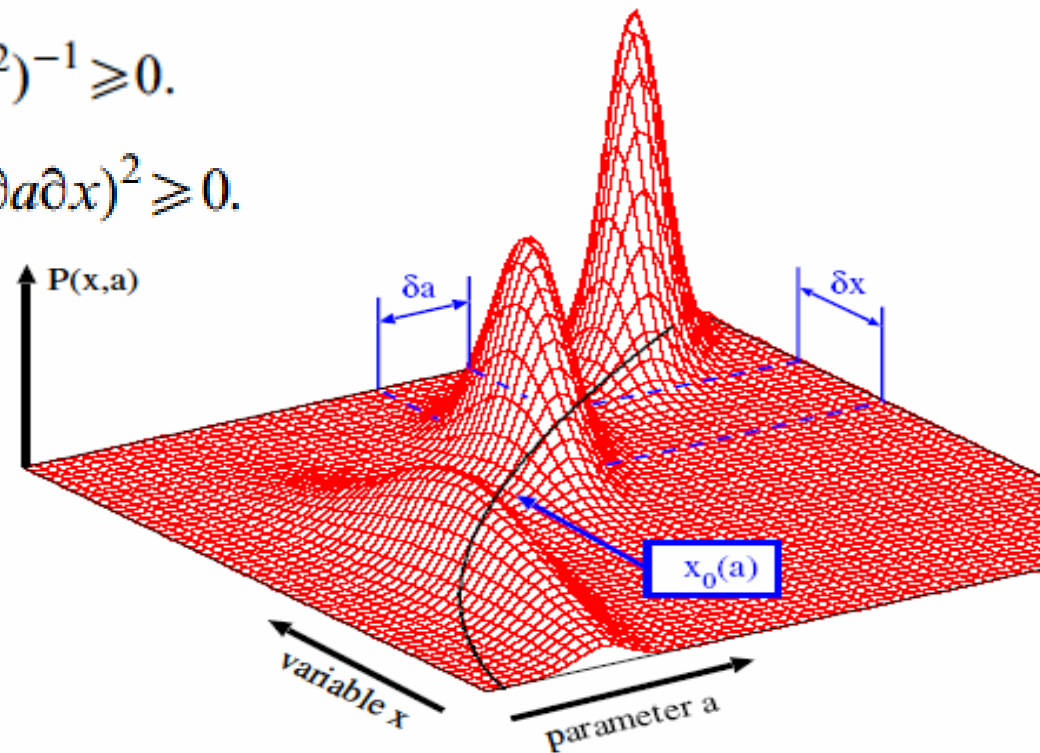
$$(\partial^2 V / \partial a^2)^{-1} \geq 0; \quad (\partial^2 V / \partial x^2)^{-1} \geq 0.$$

$$(\partial^2 V / \partial x^2)(\partial^2 V / \partial a^2) - (\partial^2 V / \partial a \partial x)^2 \geq 0.$$

Hessian condition

Up to this point pheno
(x) and geno (a) are
treated in the same way.
Then given a, the peak
(average) phenotype is
 $x_0(a)$ --function of a --

$$\partial V / \partial x|_{x=x_0} = 0$$



Phenomenological Theory for these experimental observations?

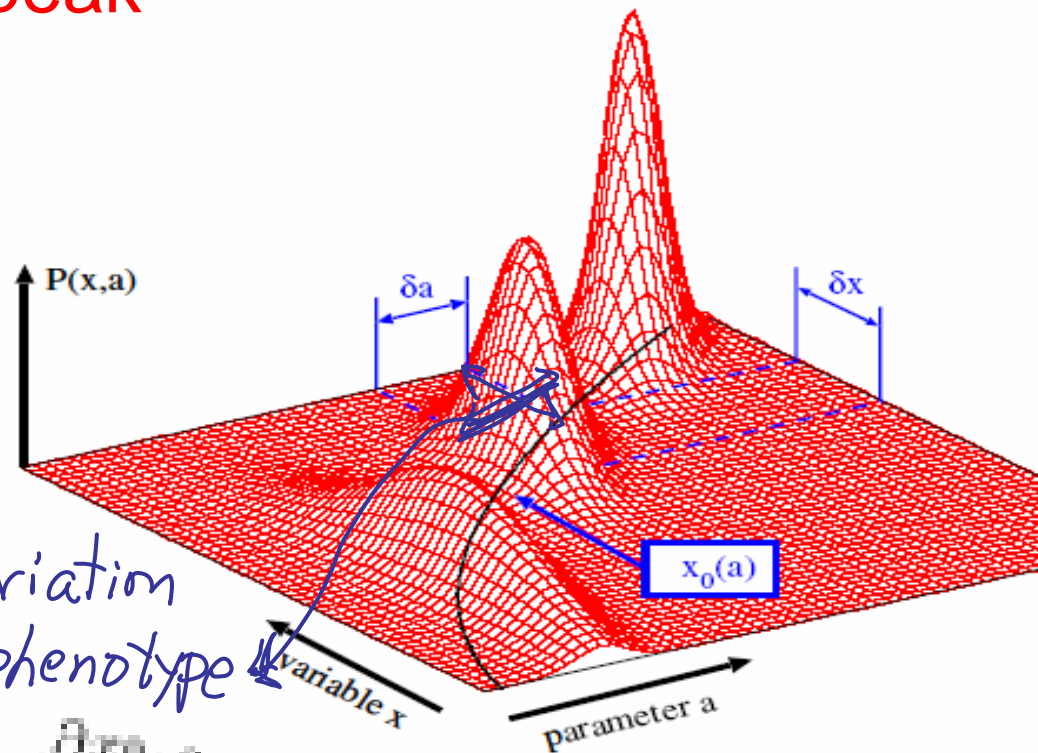
Consider $P(\text{phenotype, genotype})$ distribution $P(x, a)$
or $P(x, a) = \exp(-V(x, a))$

Condition to **keep single peak**
(evolutionary stability).

V_{ip} : $\langle \delta x \rangle^2$ of isogenic individuals

V_{ig} : variance of x due to genetic variation for the identical phenotype

$$\langle (\bar{x}_a - \bar{x}_0)^2 \rangle = V_{ig} = \langle (\delta a)^2 \rangle \left(\frac{\partial x_0}{\partial a} \right)^2,$$



$$P(x, a) = \widehat{N} \exp\left[-\frac{(x - X_0)^2}{2\alpha(a)} + \frac{C(a - a_0)(x - X_0)}{\alpha} - \frac{1}{2\mu}(a - a_0)^2\right]$$



$$P(x, a) = \widehat{N} \exp\left[-\frac{(x - X_0 - C(a - a_0))^2}{2\alpha(a)} + \left(\frac{C^2}{2\alpha(a)} - \frac{1}{2\mu}\right)(a - a_0)^2\right].$$

$$\mu \leq \frac{\alpha}{C^2} \equiv \mu_{max}.$$

$$\overline{x}_a \equiv \int x P(x, a) dx = X_0 + C(a - a_0).$$

$$V_g = \frac{\mu C^2}{1 - \mu C^2 / \alpha} \qquad \overline{V_{ip}} = \frac{\alpha}{1 - \mu C^2 / \alpha} \qquad \overline{V_{ip}} / V_g = \alpha / (\mu C^2)$$

= Ave over all populations

$$V_g \leq \overline{V_{ip}}.$$

$$V_{ig} = \frac{\mu}{\mu_{max}} \overline{V_{ip}}$$

From Stability condition $\rightarrow \underline{V_{ip} \geq V_g}$ is derived

V_g increases with the mutation rate

if the increase continues, there is critical mutation rate

μ_c at which $V_{ip} \sim V_g$

Error catastrophe \rightarrow evolution stops

Here, $V_g \neq V_{ip}$

V_g for distribution for a given phenotype

V_{ip} for all population

but for small μ

OR def V_p as average of V_{ip} ,
Then $V_p \geq V_g$

$$V_g \approx V_{ip} \approx \frac{\mu}{\mu_c} V_{ip}$$



$$\mu V_{ip} \propto V_g \propto \text{evolution speed}$$

consistent

- (i) $V_{ip} \geq V_g$ (from stability condition) (**)
 - (ii) error catastrophe at $V_{ip} \sim V_g$ (**)
 - (where the evolution does not progress)
 - (iii) $V_g \sim (\mu / \mu_{\max}) V_{ip} \propto \mu V_{ip}$
 (\propto evolution speed) at least for small μ

* * Consistent with the experiments, but,,,,,

Existence of $P(x,a)$ assumption ??;

+ Robust Evolution assumption ?? +

Why isogenetic phenotypic fluctuation leads to robust evolution?

(**) to be precisely V_{ig} , variance those from a given phenotype x : but $V_{ig} \sim V_g$ if μ is small

- ??? to the theory
 - $P(x,a)$ rather than conditional probability (TRICK)
- “Genetic-Phenotypic correspondence”
- what phenotype can vary \leftrightarrow
what gene can change
- fluctuation of variable (micro) vs
variation of equation (genetic evolution)
(cf Waddington’s genetic assimilation)

Q: Why error catastrophe when $V_g > V_{ip}$?

Robust evolution is possible only under noise

-counterintuitive ;it says phenotype noise is important

→ gene-net model

Gene expression dynamics model::

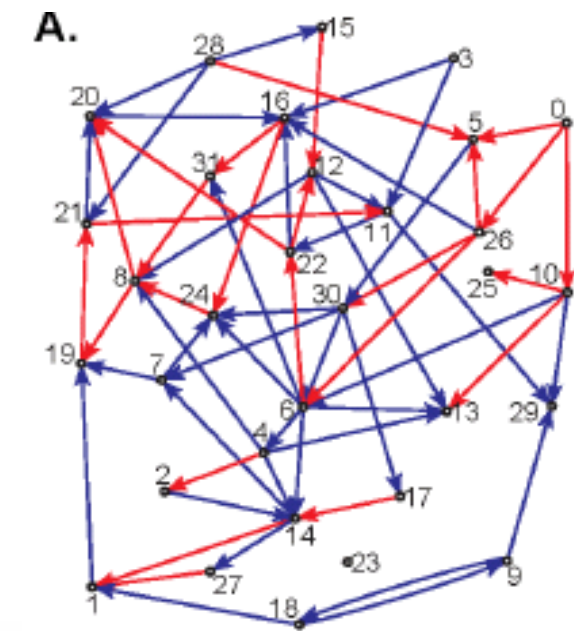
Relevance of Noise to evolution?

Simple Model: Gene-net (dynamics of stochastic gene expression) \rightarrow on/off state

x_i – expression of gene i :
on off

$$dx_i/dt = \tanh\left[\beta \sum_{j>k}^M J_{ij}x_j\right] - x_i + \sigma\eta_i(t),$$

$$\langle \eta_i(t)\eta_j(t') \rangle = \delta(t-t') \cdot \delta_{ij}$$



Gaussian white

M ; total number of genes, k : output genes

Noise strength σ

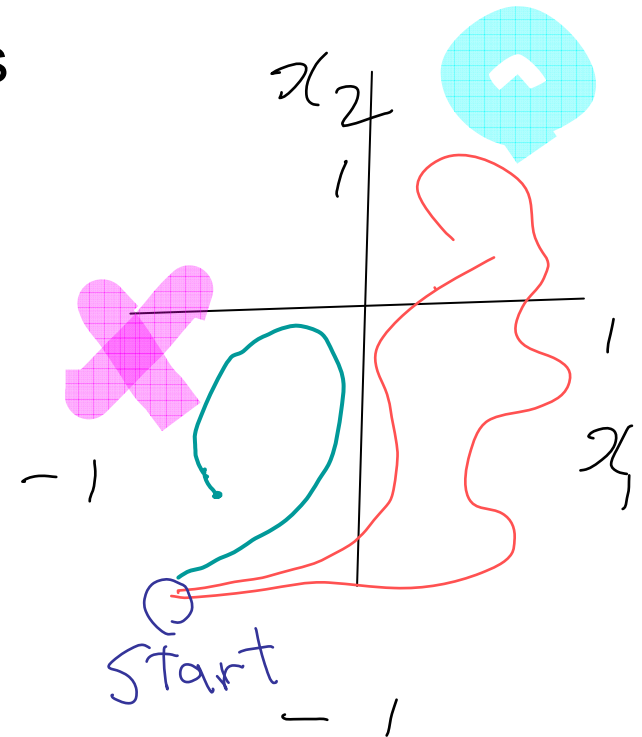
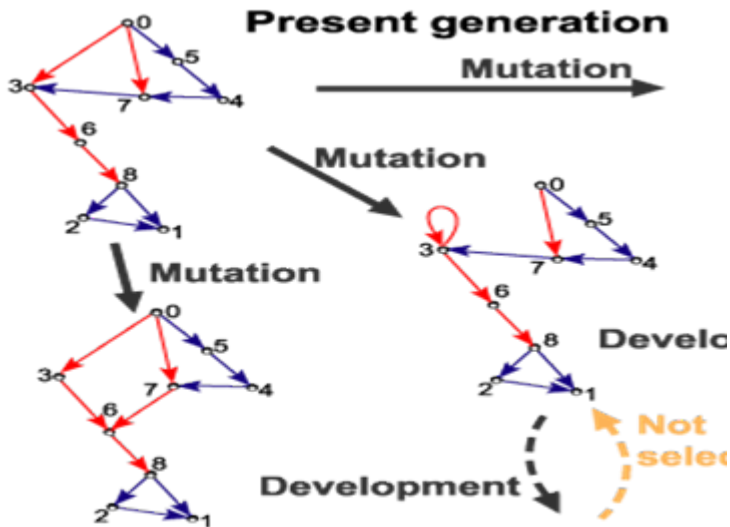
- Fitness: Starting from off of all genes, after development genes x_i $i=1, 2, \dots, k$ should be on (Target Gene Pattern)

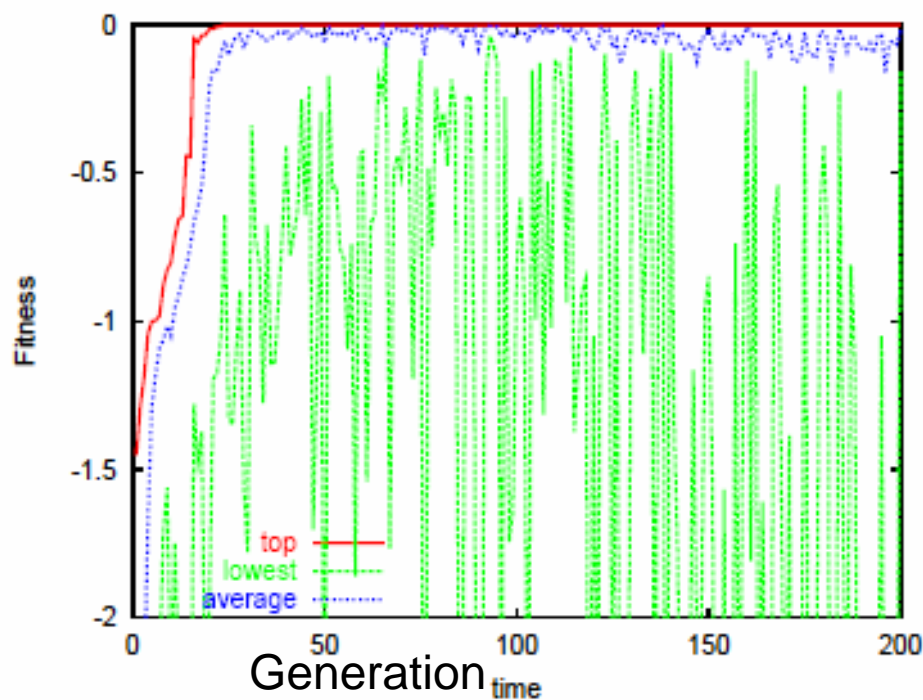
Fitness $F = - (\text{Number of off } x_i)$

Genetic Algorithm

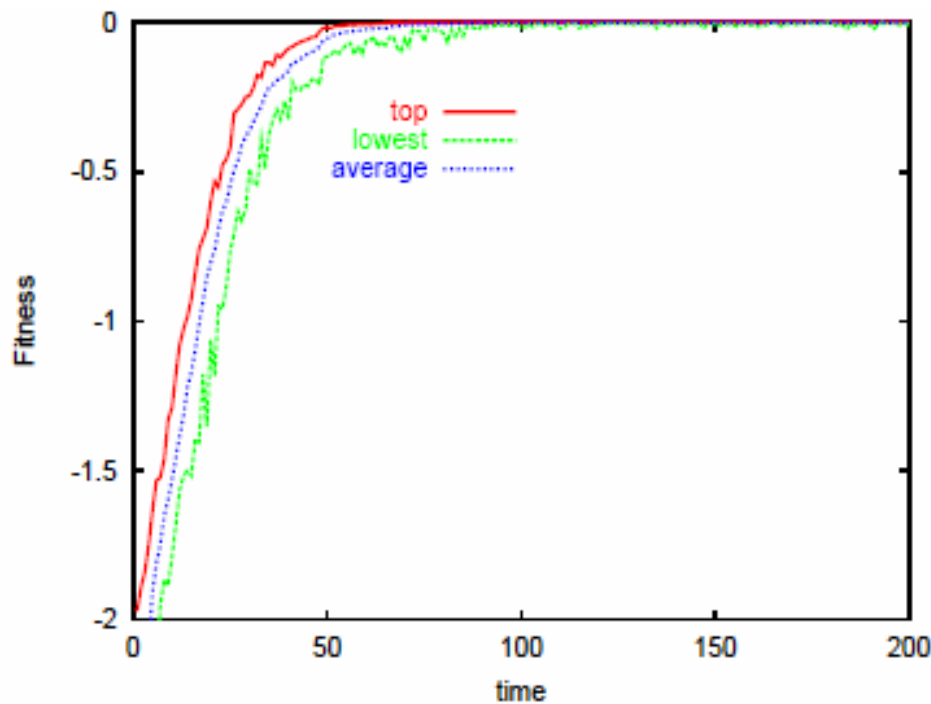
Mutate networks and Select those with higher $\langle F \rangle$

Choose top n networks among total N ,
and mutate with rate μ to keep N networks





Low noise case:
top reaches the fittest
but low-fitness
mutants remain

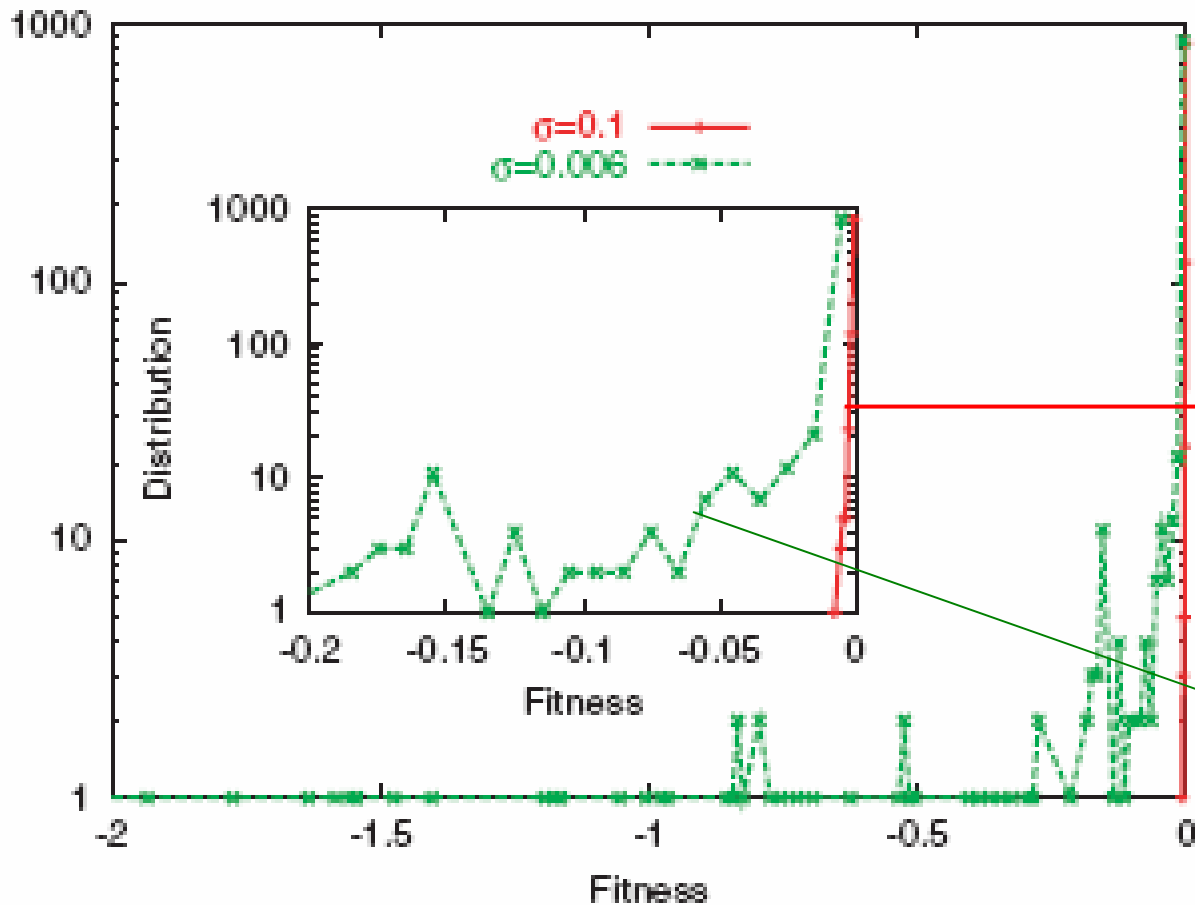


High Noise case:
top-lowest
All reach the fittest

Result of evolution

Top:reaches the fittest
Lowest;cannot evolve
for low noise(σ)

Distribution

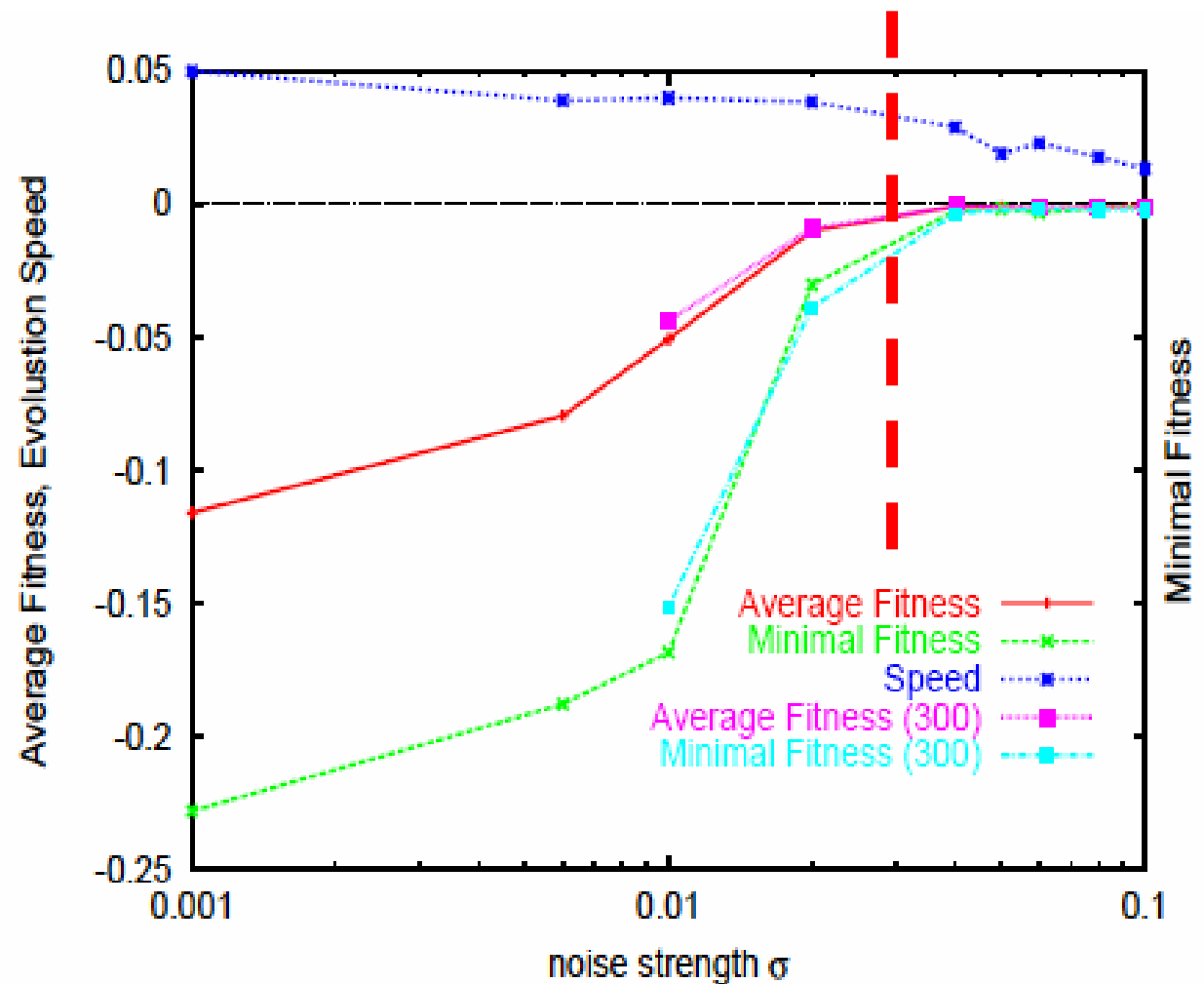


$\sigma > \sigma_c$

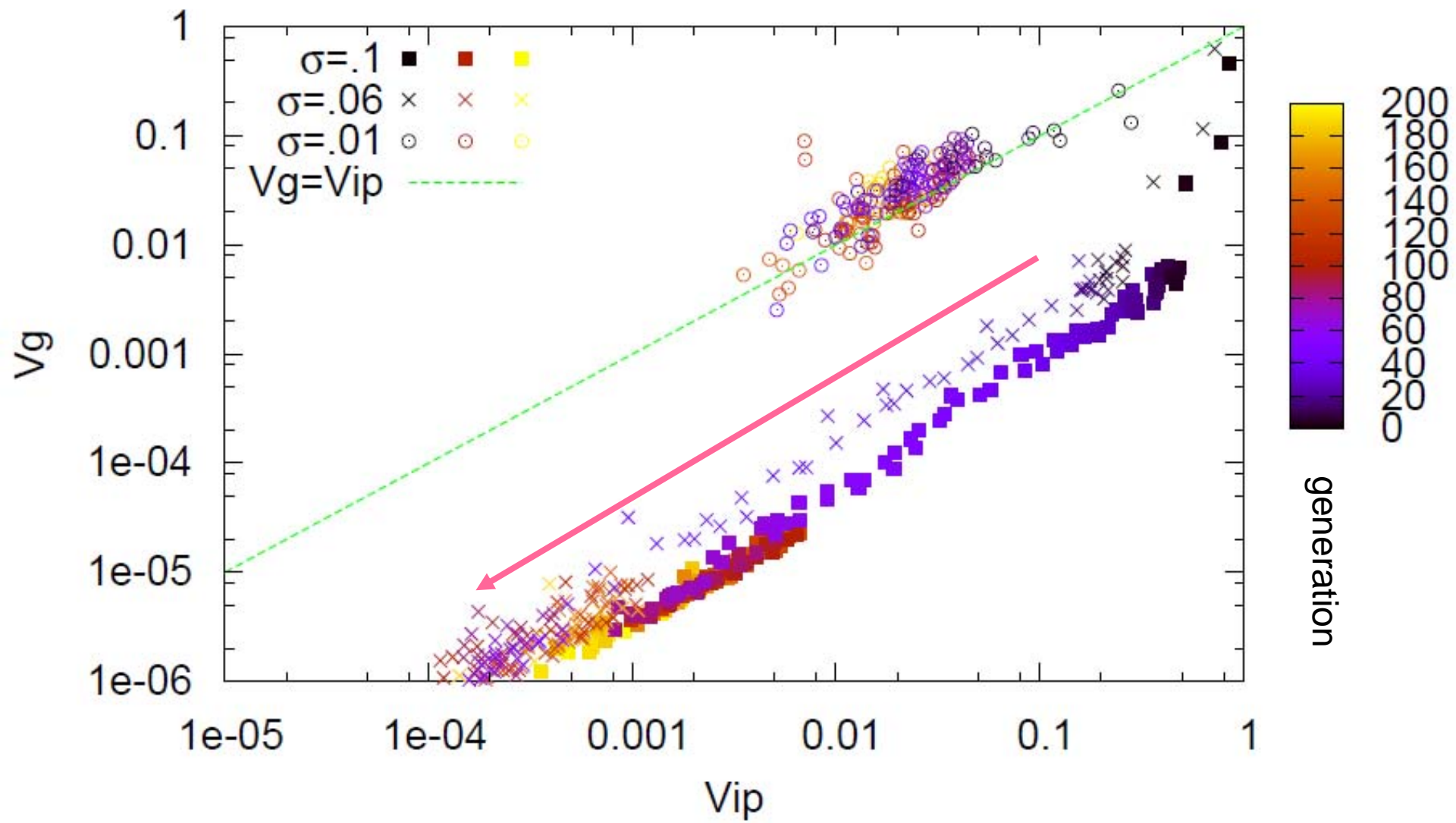
$\sigma < \sigma_c$

Fitness Distribution

$\sigma < \sigma_c$ --low fitness mutants distributed
 $\sigma > \sigma_c$ — eliminated
 through evolution



**Existence of critical noise level σ_c
below which low-fitness mutants accumulate
(error catastrophe)**

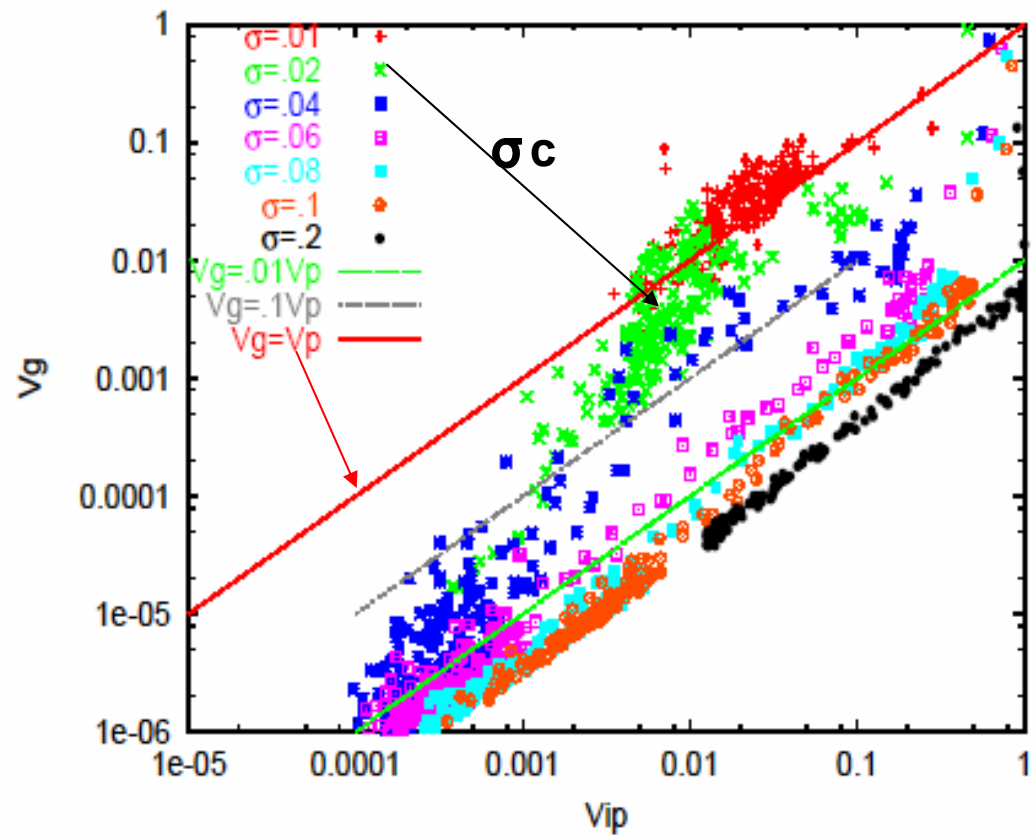


(1) $V_{ip} \geq V_g$ for $\sigma \geq \sigma_c$

(2) $V_g \rightarrow V_{ip}$
as $\sigma \rightarrow \sigma_c$

(3) evolution progresses
only for $V_{ip} \geq V_g$

(4) $V_{ip} \propto V_g$
through evolution course (✓)



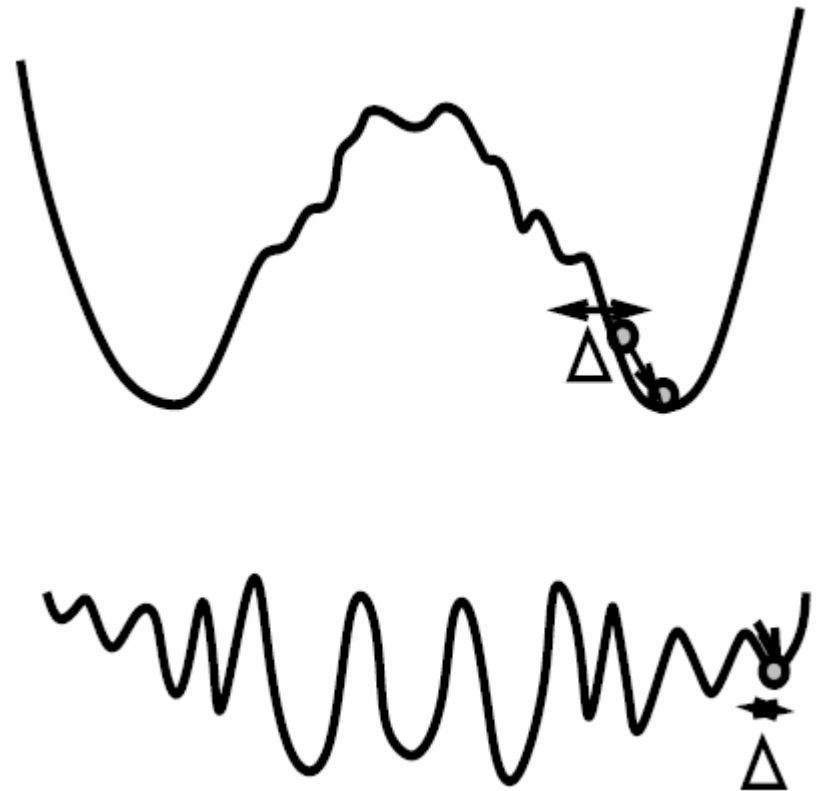
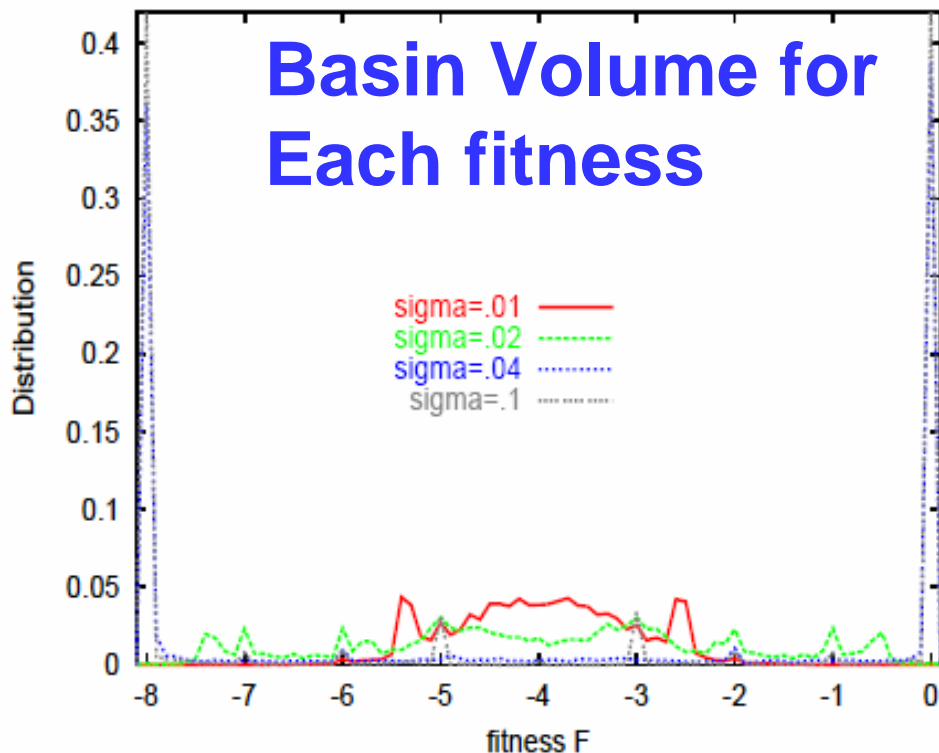
Theory confirmed

KK, PLoSOne, 2007

Why?; difference in basin structure

$\sigma > \sigma_c \rightarrow$ large basin for target attractor
(robust, Δ (distance to basin boundary) \uparrow)

$\sigma < \sigma_c \rightarrow$ only tiny basin around target orbit
 Δ remains small



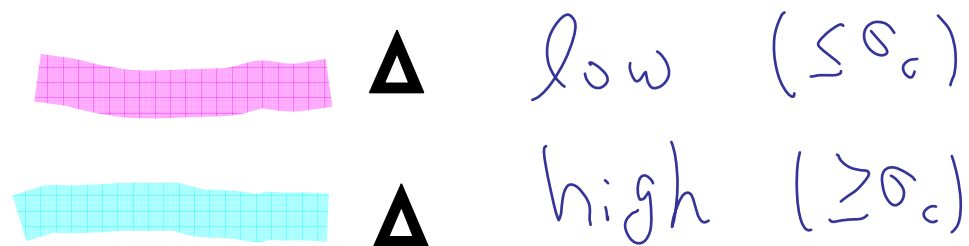
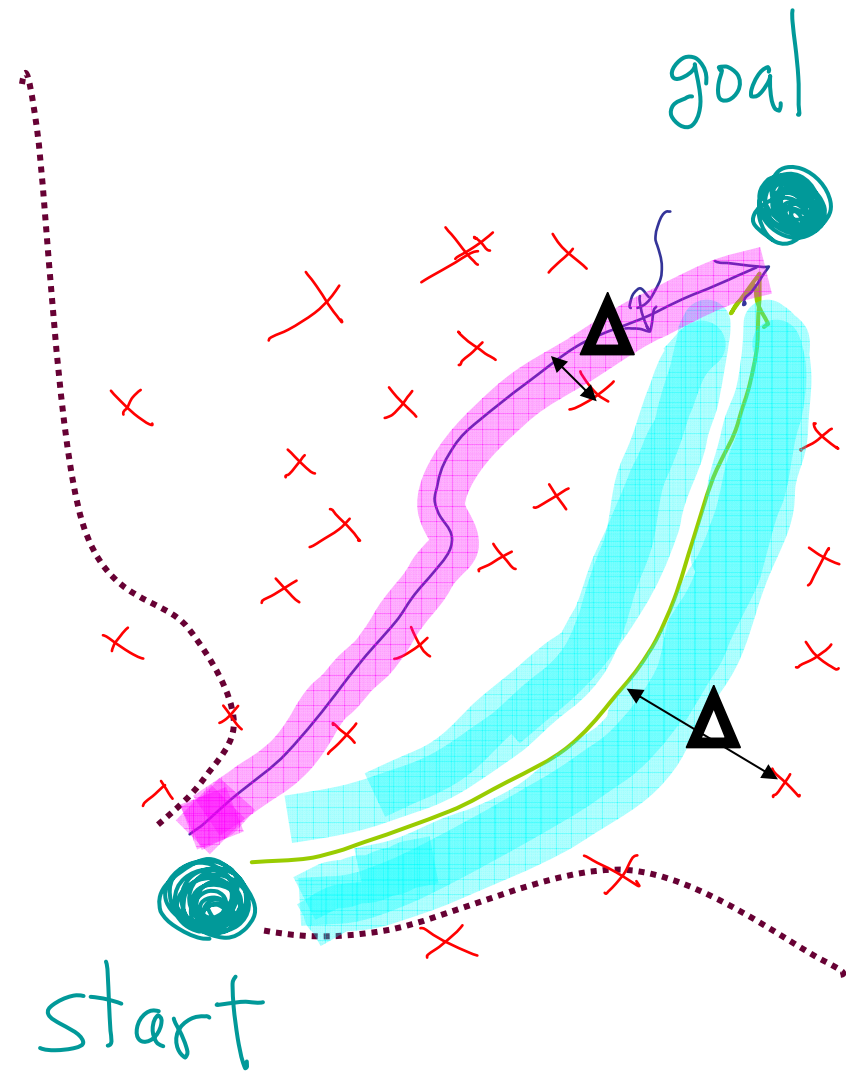
\rightarrow Global constraint to potential landscape(funnel?)

why threshold?

choose paths to avoid turning
pts within σ (noise)

Mutation \rightarrow touches turning
points within range of μ

small $\sigma \rightarrow$
an orbit with small Δ
can reach the target



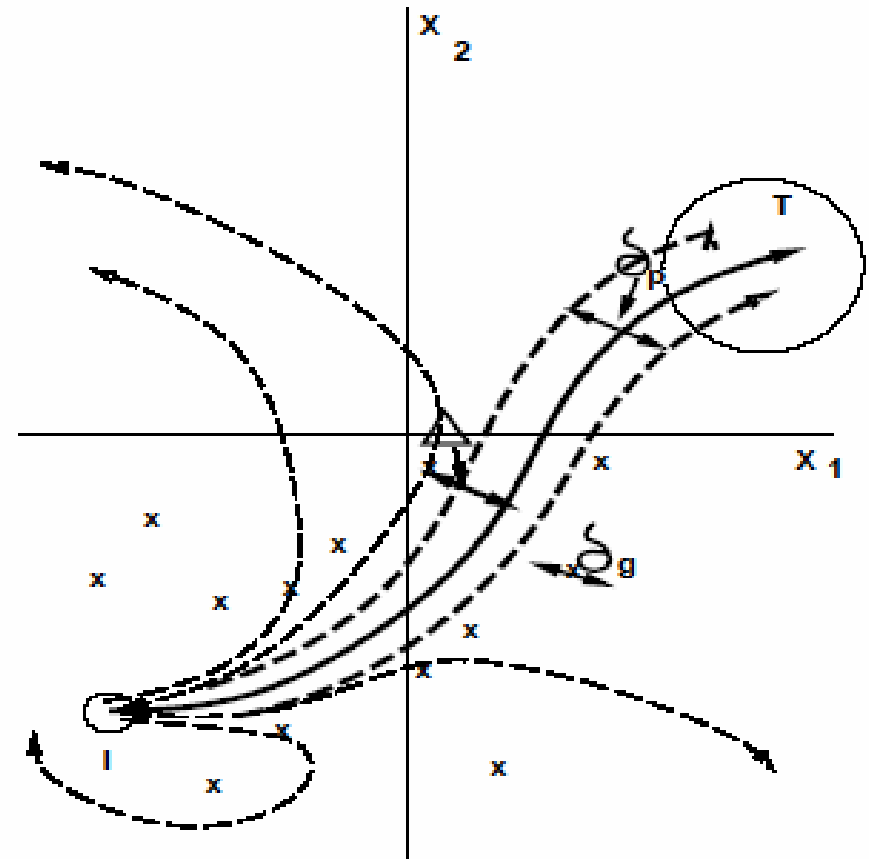
Deviation of basin
 boundary (turning points)
 by Noise $\rightarrow \delta p$
 by Mutation $\rightarrow \delta g$

$$V_g \sim (\delta g / \Delta)^2$$

$$V_{ip} \sim (\delta p / \Delta)^2$$

Δ increases
 \rightarrow robustness
 increases
 if $\delta g > \delta p$,
 mutation destroys
 the history

$\rightarrow V_{ip} > V_g$ necessary
 for evolution of robustness



$\Delta \sim$ distance to turning points
 (basin boundary)

- Genetic robustness is increased for network evolved under higher noise

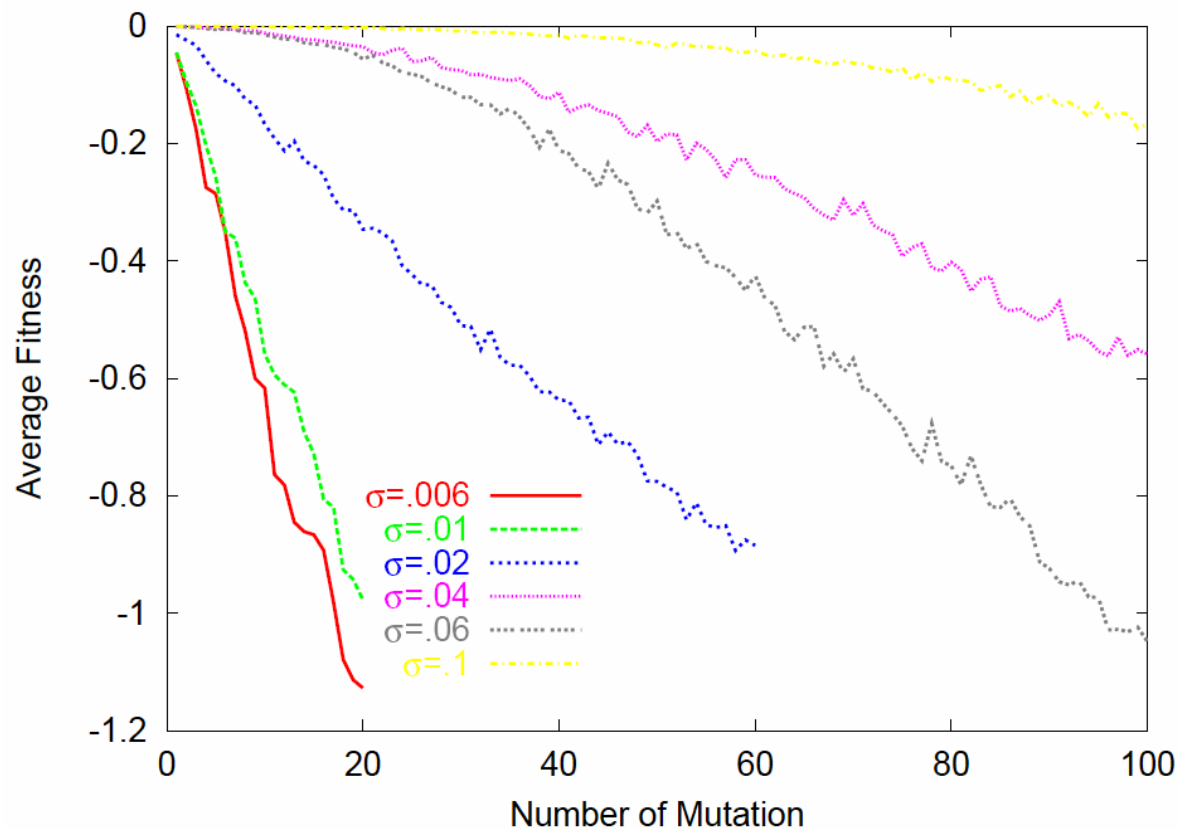
- Increase in genetic robustness to mutation

fraction of fitted state for n-mutants

$$F = -c(\sigma) m ;$$

$$C(\sigma) > 0 \text{ if } \sigma < \sigma_c$$

$$C(\sigma_c) = 0$$



Discussion: Evolution of Robustness

- Robustness ----- Insensitivity of Fitness (Phenotype) to system's change

← against noise during 'developmental process

← against parameter change by mutation

- Developmental Robustness to noise ---- V_p

- Robustness to mutation in evolution ---- V_g

For $\sigma > \sigma_c$, both decrease, i.e., robustness

Noise is necessary for evolution of robustness

$V_p \propto V_g \rightarrow$ Developmental robustness and genetic (evolutionary) robustness are linked (or embedded)

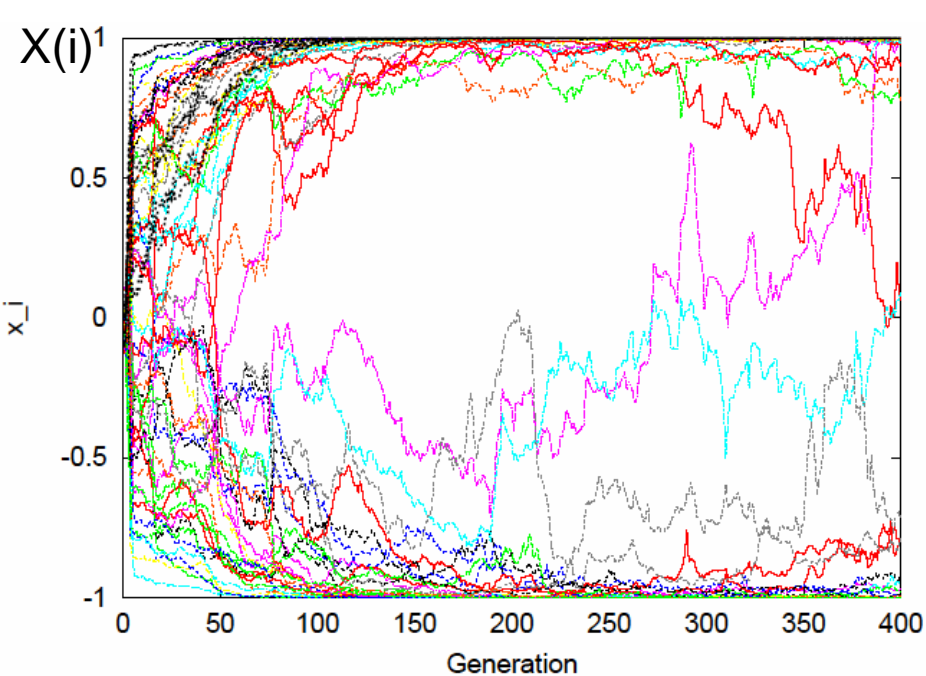
WADDINGTON genetic assimilation

(cf. Ancel-Fontana J Exp Zool B 2000

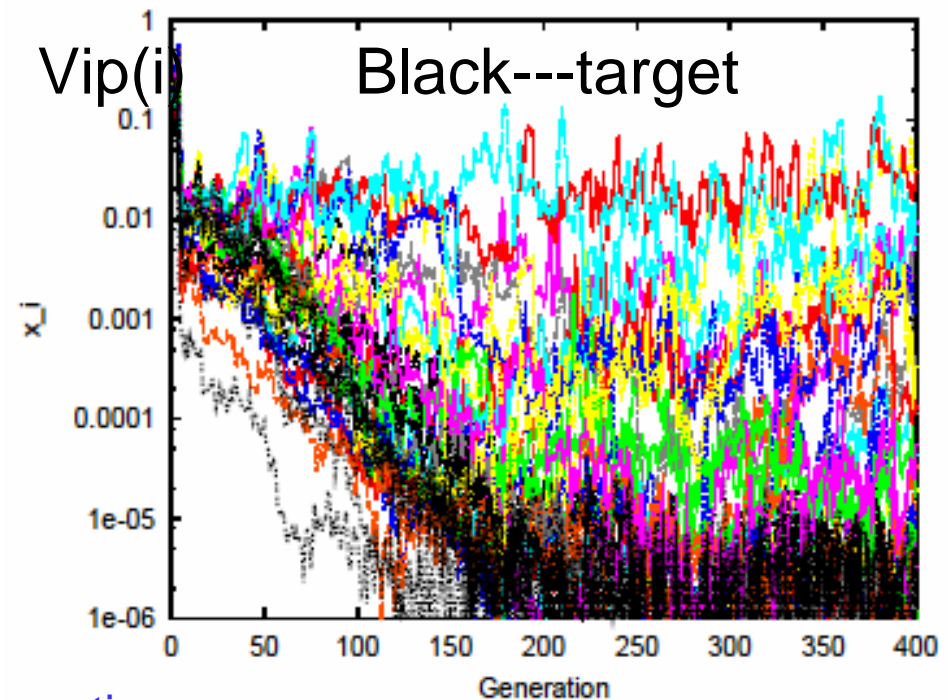
A Wagner et al, PLoS Comp Biol 2007)

Formation of smooth dynamics ; how ?

Consolidation of non-target gene expressions



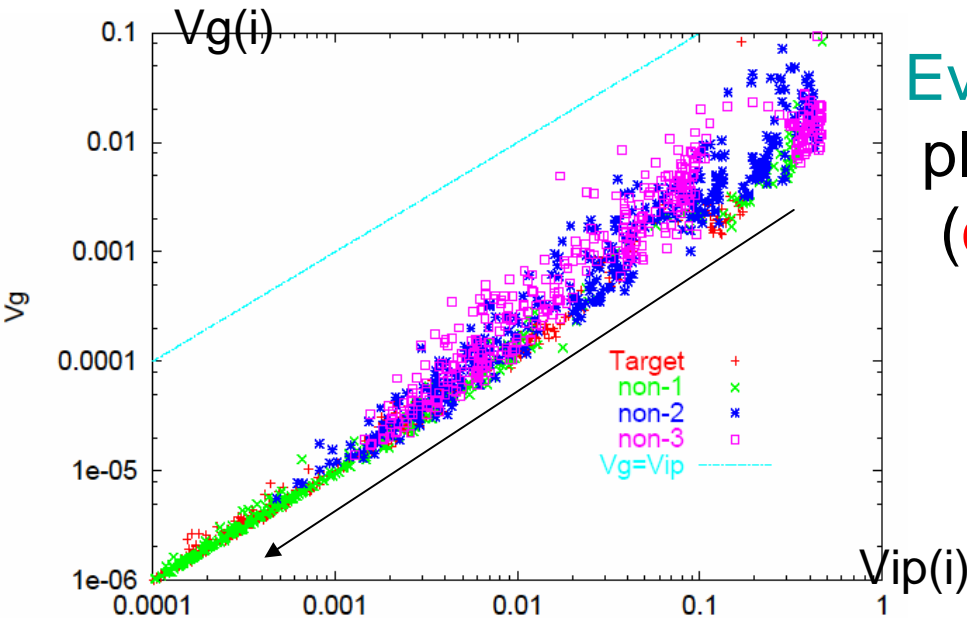
Generation



Expression of many non-target gene expressions are fixed successively:

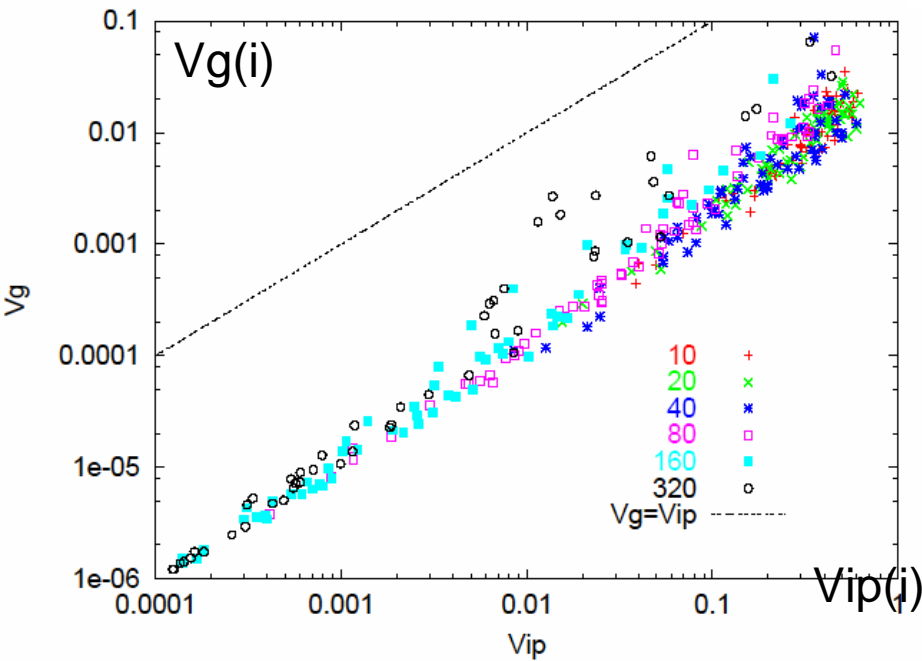
- variance of many gene expressions i - genetic $Vg(i)$ & epigenetic $Vip(i)$ decrease successively ;

Further Surprise; Universal relationship over all genes?



Evolutionary course of $(Vip(i), Vg(i))$
plot for several genes I
(color –different gene i)

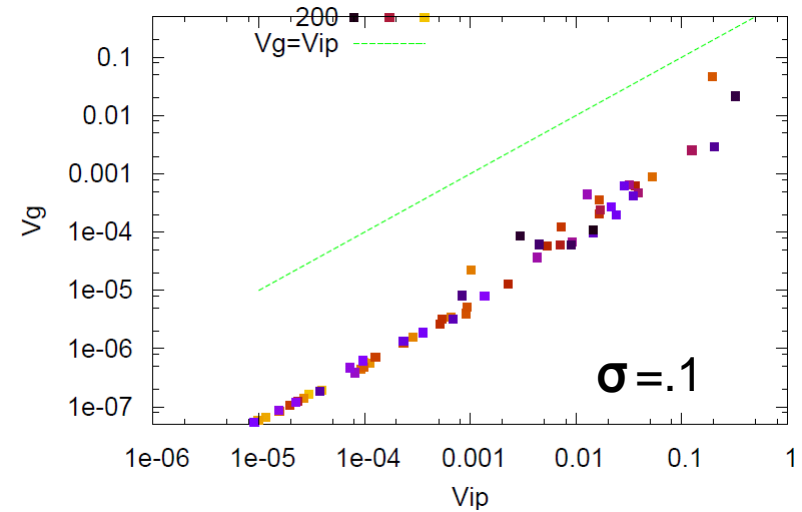
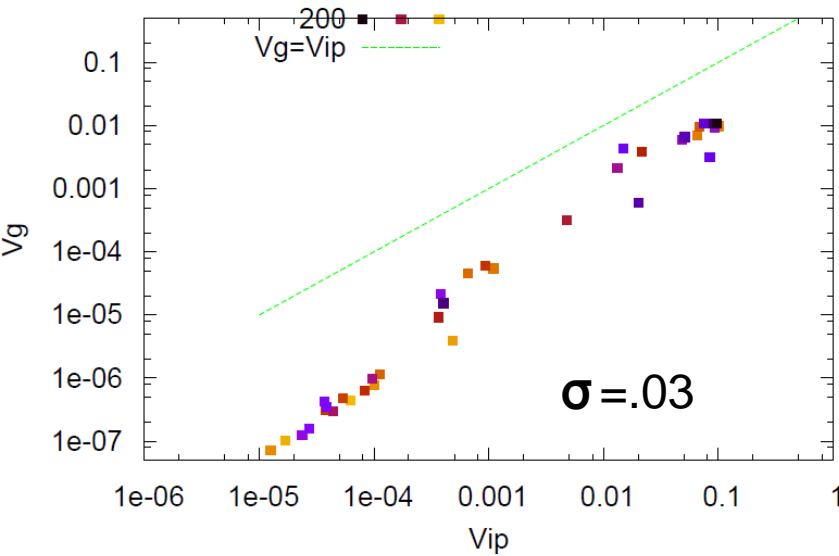
Approaches proportionality
relationship



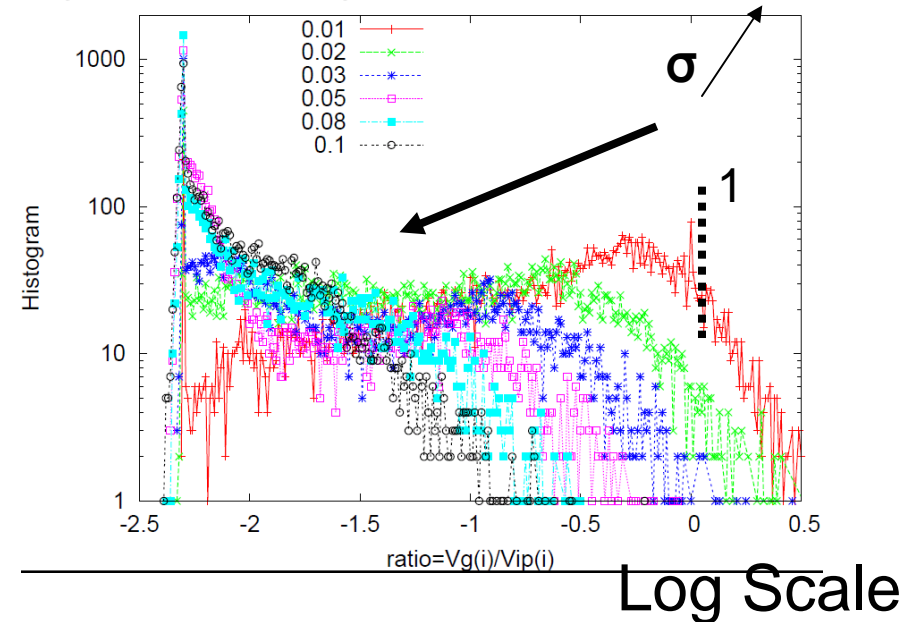
Snapshot plot of all gene
expression variances ;
(color different generation)

Approach a unique line
for all genes(?!)

Vip(i)-Vg(i) relationship over genes; snapshot at 200th generation



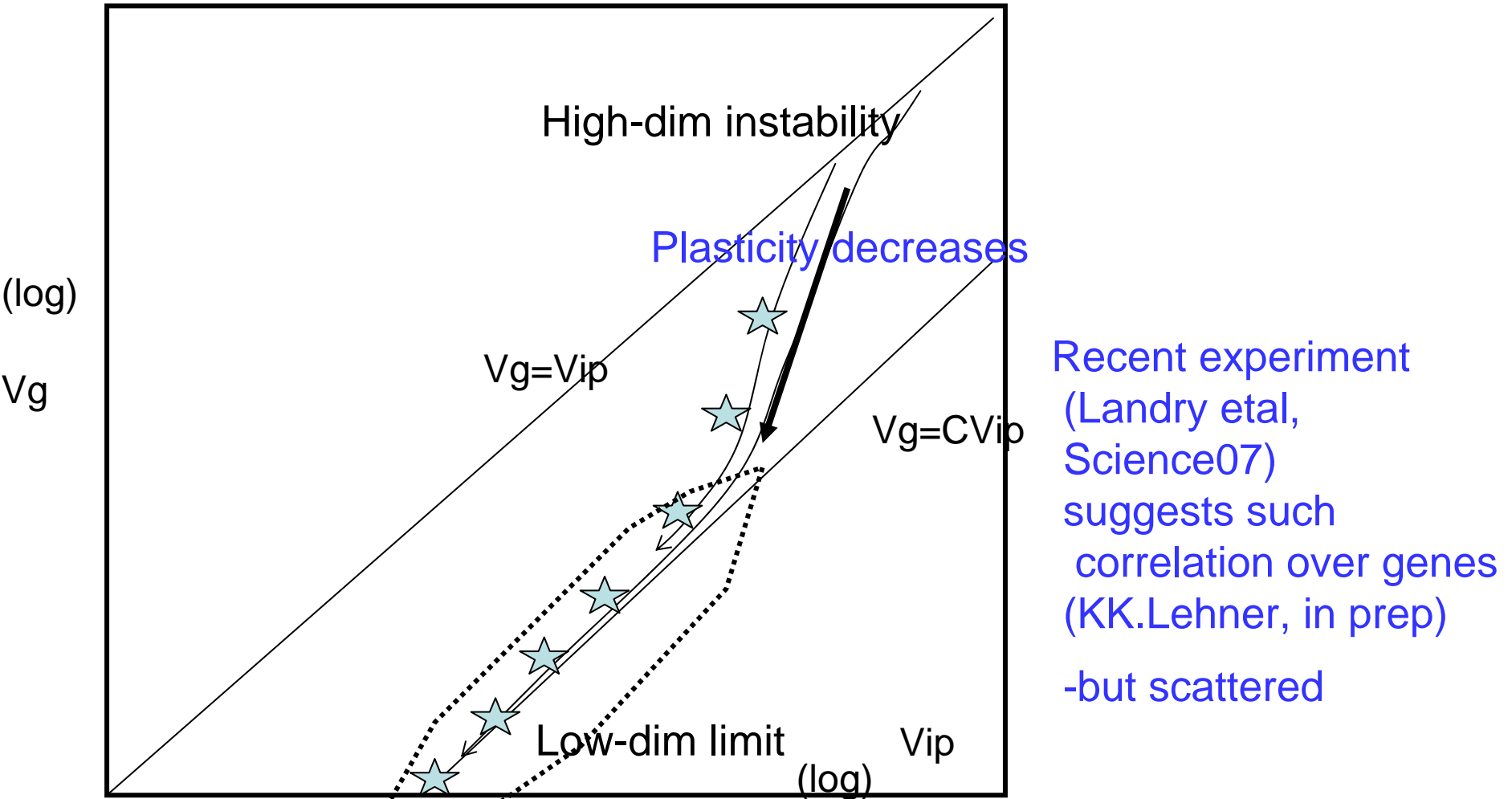
Histogram of $Vg(i)/Vip(i)$



As noise increases, evolved dynamics are more robust, to lose plasticity

Plasticity $\sim Vg(i)/Vip(i)$
 Fraction of plastic gene expression decreases as σ

‘universal line is approached ‘over genes’ and ‘over generations’



Universal proportion coefficient over genes akin to **fluctuation-dissipation relation** ----- result of consistency of each gene expression dynamics and fitness as collective state (cf Einstein)

Through directed evolution; fluctuations decrease

(**Model, experiments, theory, i.e., increase of robustness through evolution.)

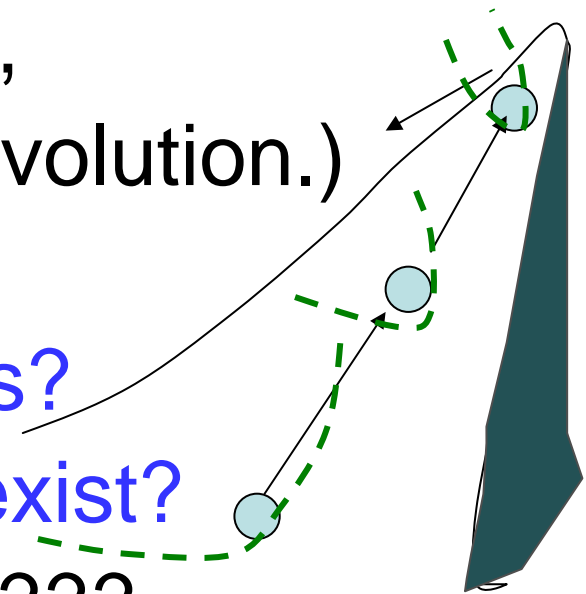
Then, evolution slows down..

↔ How Evolution continues?

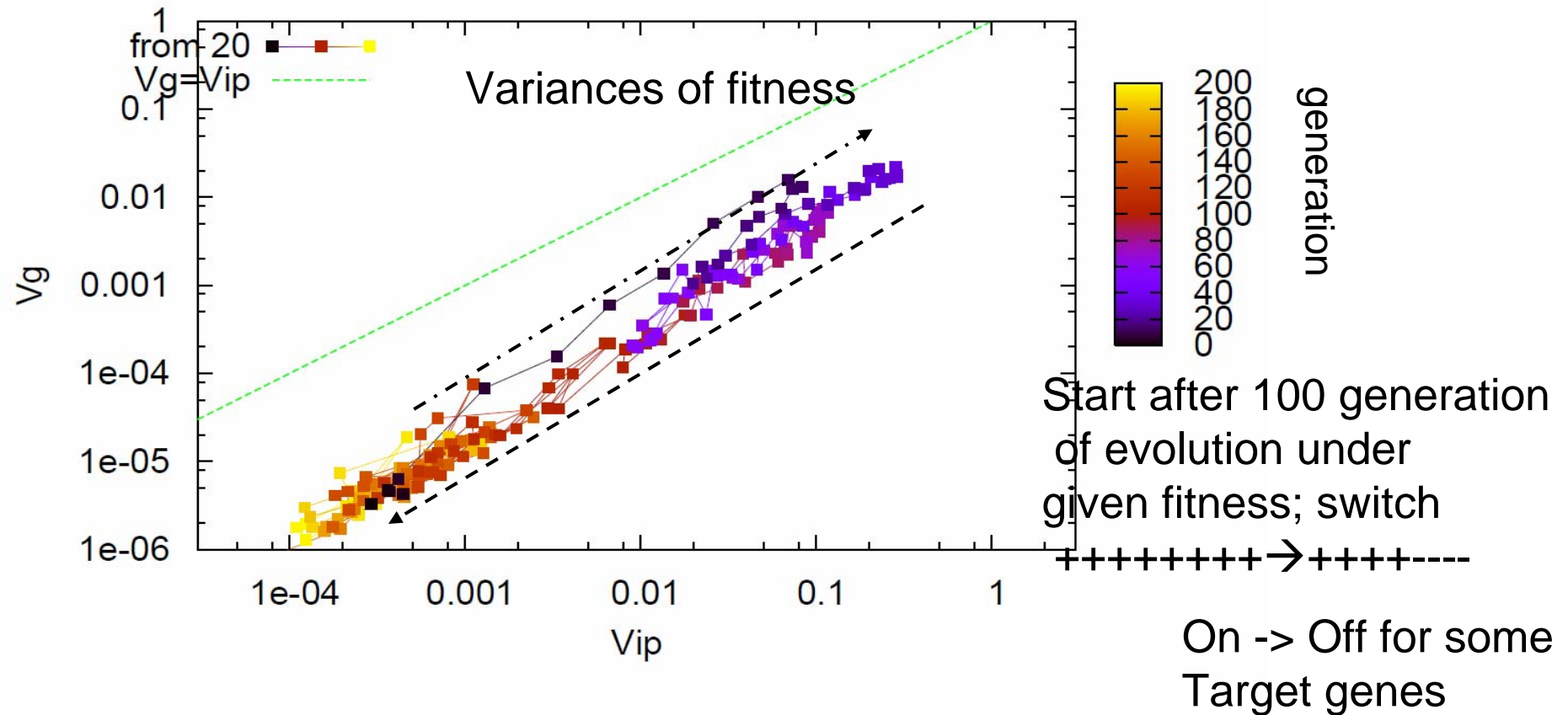
Why Large Fluctuations exist?

?? Is there regain of fluctuations????

- Experimentally Observed: Appearance of mutants with large fluctuations at further evolution. (← interference with other processes) (Ito, Toyota, KK, Yomo, submitted)
- → Restoration of Plasticity



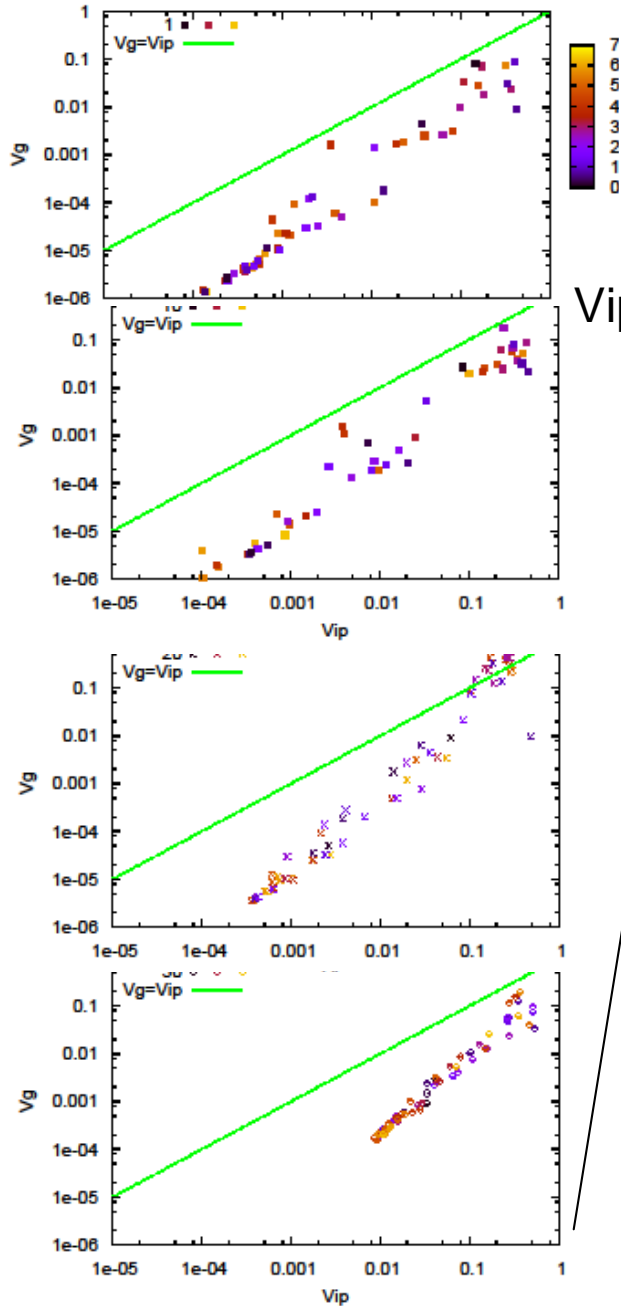
In fixed environment/fitness, plasticity decreases.
 When environmental condition is **switched** in the model
 → fluctuation once **increases to regain plasticity**
 (**evolvability**) and then decreases



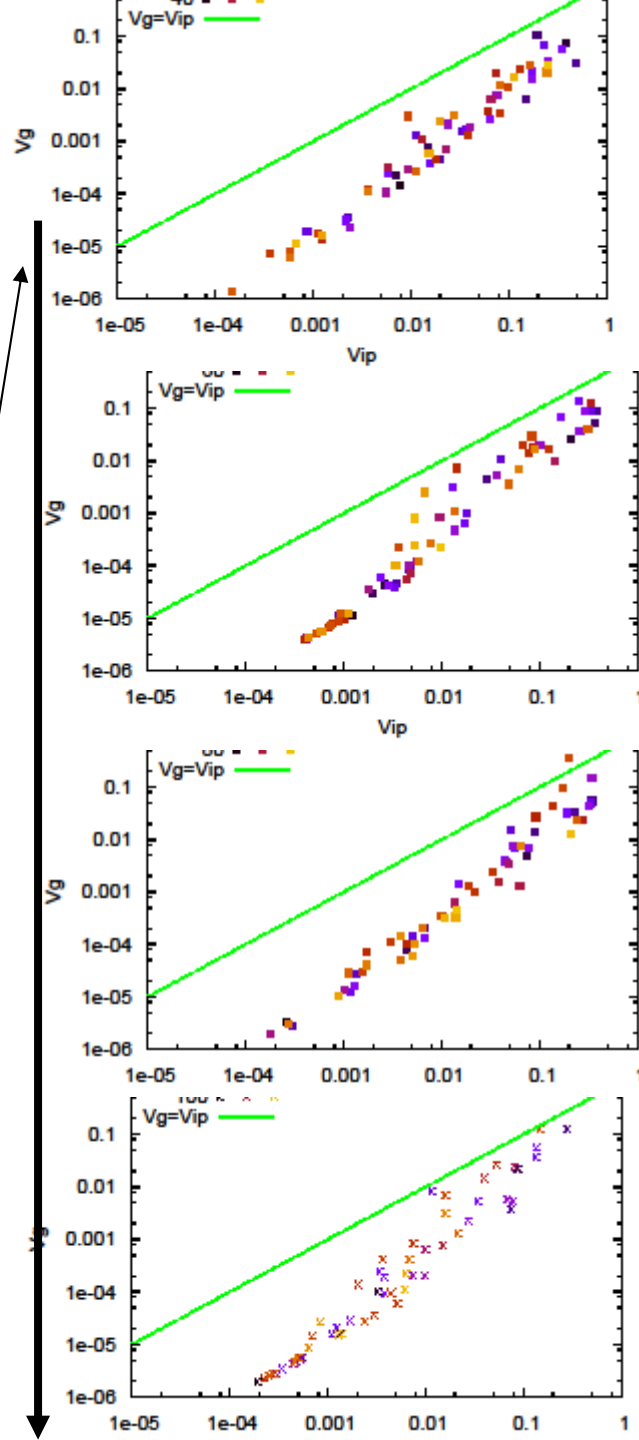
In a fluctuating environment, fluctuation (plasticity) is sustained

(Increase of fluctuation in bacterial evolution; Ito-Toyota-KK-Yomo)

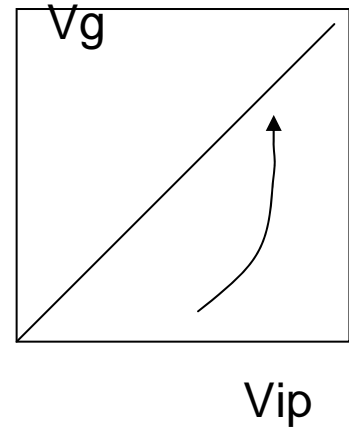
$V_g(i)$



$V_{ip}(i)$



increase
instability to
approach $V_g \sim V_{ip}$



V_{ip}/V_g
Works as
a measure of
biological
plasticity

Generation after switch

- Generality of our result; For a system satisfying:

(1) fitness is determined after developmental dynamics

(2) developmental dynamics is complex
(catastrophic pts leading to error are distributed)

(3) effective equivalence between mutations and noise with regards to the consequence to fitness

(→ genetic assimilation by Waddington)

Symbiotic Sympatric Speciation

Kk,Yomo2000
ProcRoySoc

- So far, 'fluctuation' – single-peaked distribution
- Speciation → change to double peaked distribution
- ** **Allopatric vs Sympatric (S fundamental? Difficult?)**
- Our scenario for sympatric speciation (confirmed by several models):
 - (1) Isologous divesification (**interaction-induced phenotype differentiation**);
homogeneous state is destabilized by the interaction
e.g., by the increase in resources
 - (2) **Amplification of the difference through geno-pheno relation**
Two groups form symbiotic relationship, and coevolve
 - (3) **Genetic Fixation and Isolation of Differentiated Group**
consolidated to genotypes

Isologous Diversification:

internal dynamics and interaction : development phenotype

instability

distinct phenotypes

interaction-induced

$$\frac{dx^m}{dt} = f_m(x^1, x^2, \dots, x^k)$$

Example: chemical reaction network

specialize in the use of some path

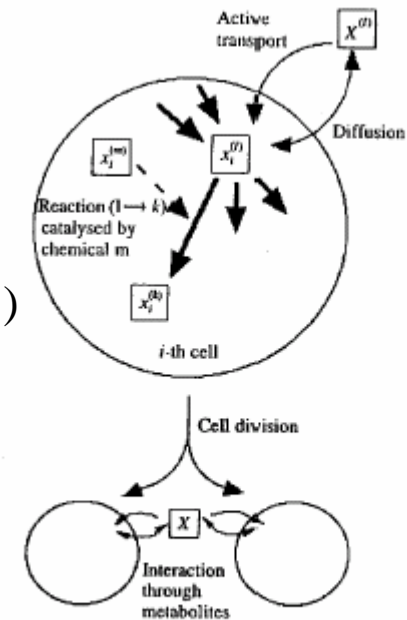
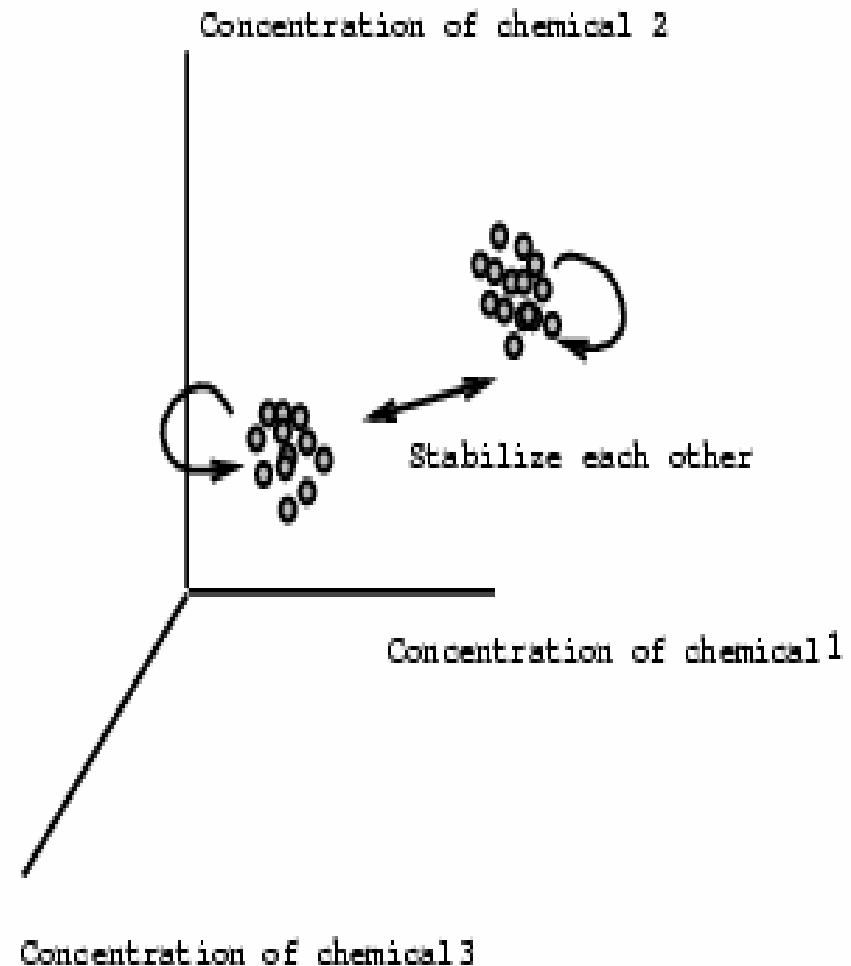
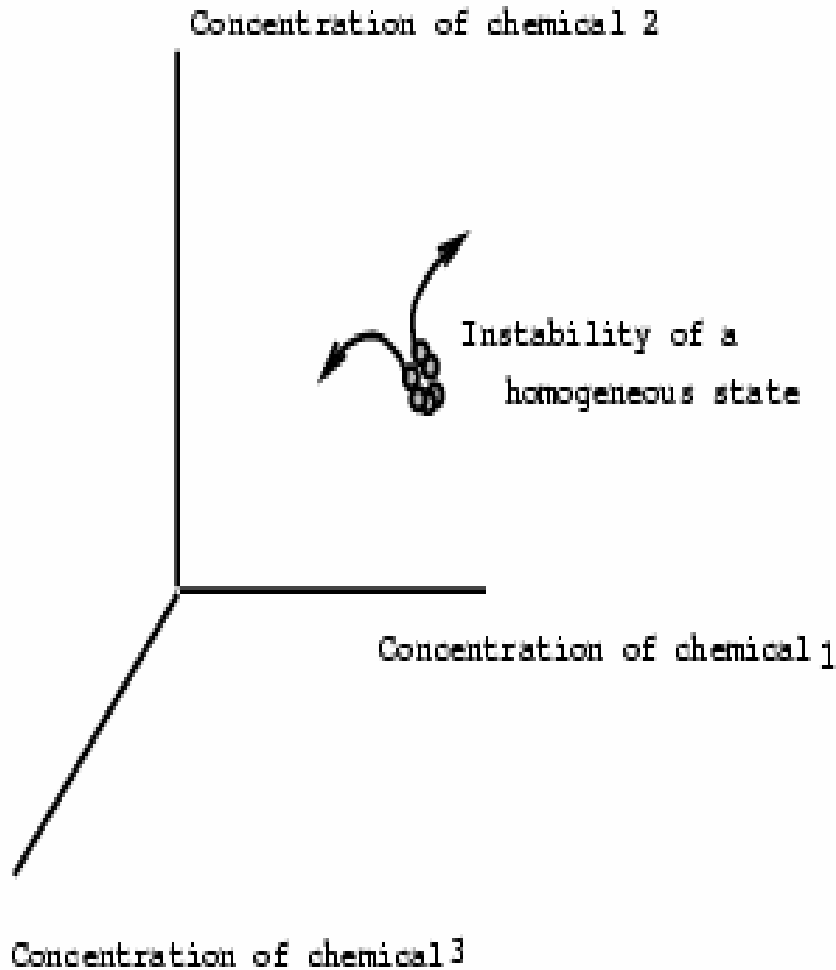


FIG. 1. Schematic representation of our model. See the appendix for the specific equation of each process.

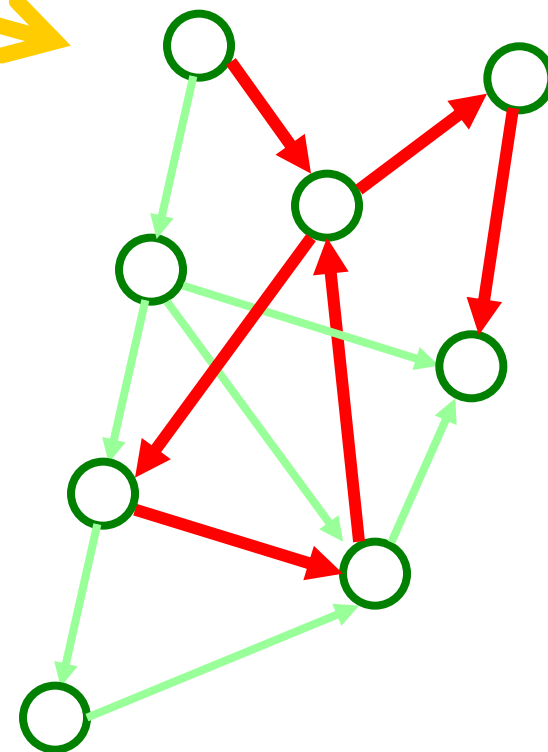
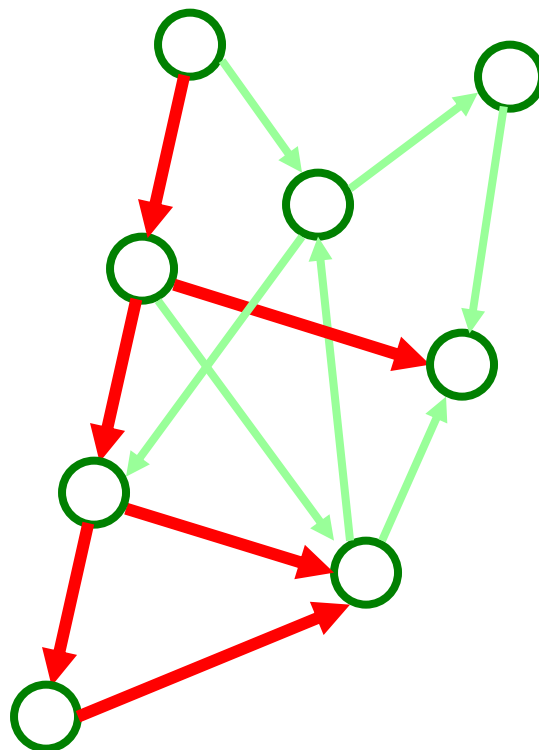
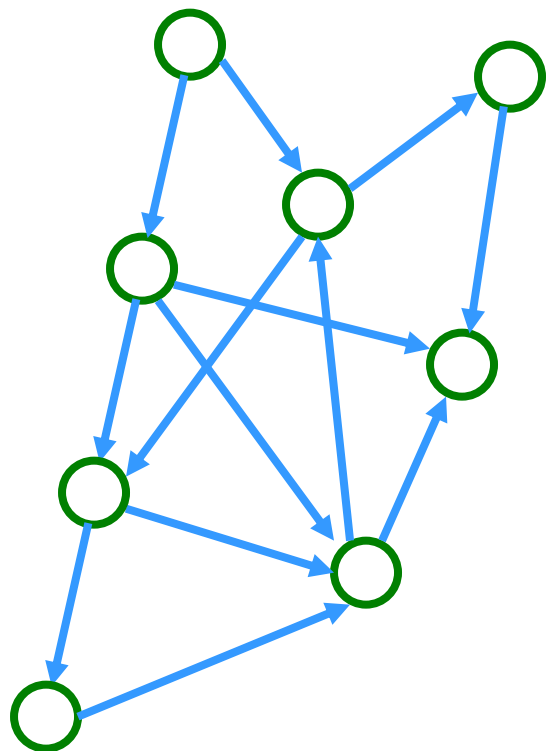
Study of coupled dynamical systems (globally coupled map) etc.,
differentiation??

→ With the increase of the number



Distinct types are formed through instability in 'developmental dynamics' and interaction (both types are necessary)

Differentiation of role; use of different paths



Model with Evolution :

Each unit Phenotype :: Variable $X = (X_1, X_2, \dots, X_k)$

Gene :: Parameter in the model e.g., reaction rate
 (g_1, g_2, \dots, g_k)

Parameter  Variable (dynamical systems)
 $X(t=0) \rightarrow X(t)$

Reproduction when maturity threshold condition
(given by X) is satisfied

Mutation ---- small change in parameter in reproduction

Competition for survival:

(remove some units (either randomly or under some condition))

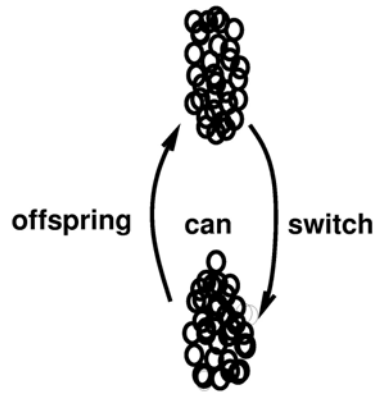
P (phenotype)



G (Genotype) a)

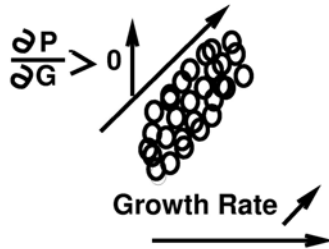
P

Differentiation to two types



G b)

P



Growth Rate



G c)

P

Recursive
without the
other group



Recursive
without the
other group



G d)

Characteristics of the Symbiotic Sympatric Speciation

- *Valid (possible) in the presence of strong interaction

- *Robust speciation; two groups coevolve; works under sexual and asexual cases as well (indeed, hybrid sterility is resulted)

- *Genetic separation always follows if there appears interaction-induced phenotypic differentiation

- *Relevance of the phenotypic differentiation, rather than genetic change, to genetic diversification (Baldwin effect or genetic assimilation → speciation)

Plasticity in phenotype from loose dynamics → interaction-induced phenotypic differentiation

Consolidated to Genes → Mating → Allele-correlation, Space..

Prove the above scenario?? From observation-- often remains a guess...

Real experiment wanted:

E Coli ; interaction-induced phenotypic differentiation observed

Evolution (Yomo's group)

genetic fixation --- not yet; but

coexistence of diverse types by 'crowded' condition is confirmed

Spontaneous Adaptation

- For all possible changes in environment, signal transduction network is already provided?
- Or, is there any general (primitive) mechanism to make spontaneous adaptation?
- → Constructive Experiment with artificial Gene and theory assuming only growth condition and stochasticity

Questions

(1) All chemicals have such large fluctuations?
Important ones are protected??

Origin of heredity (genetic information)

Minority control mechanism

(KK,Yomo JtheorBiol.2002)

(2) Large phenotypic fluctuation →
relevance to biology ?

ans. **evolution** (Sato et al., PNAS, 2003)

adaptation,

differentiation....

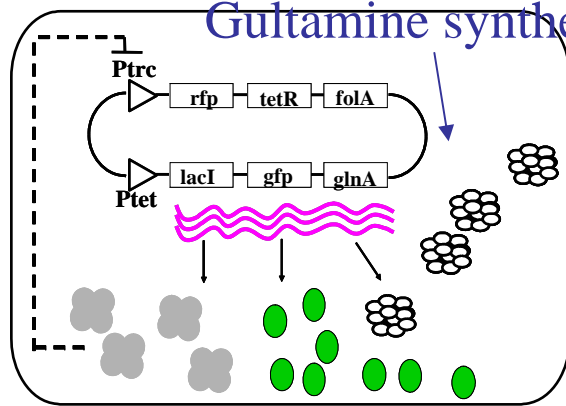
(ex) Adaptive response without signal transduction

Unexpected; beyond designed
Selection of preferable state

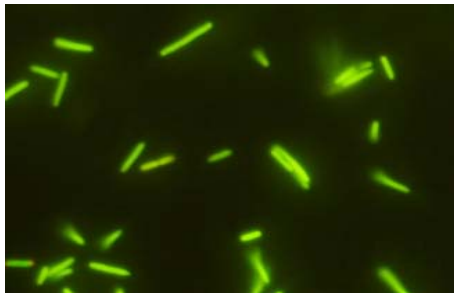
Embedded gene network

Phenomenological theory of attractor selection

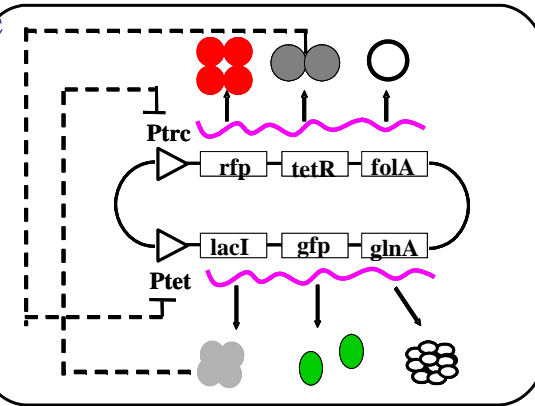
Glutamine synthetase



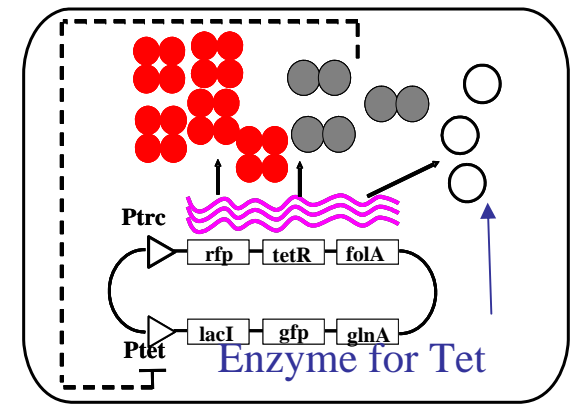
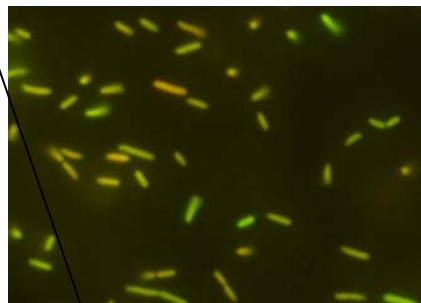
Env. Without glutamine



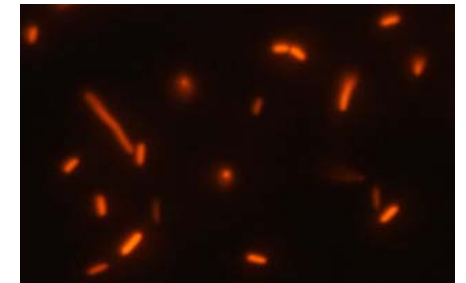
Mutual inhibition



Rich environment



Env. Without Tetrahydro..



fluctuation

Metabolic activity

Theory of attractor selection by
activity and noise

- Embedded network: each of the two can be selected equally. However, 'good' attractor in each environment is selected. Why?
- Due to hidden signal network?
NO!: verified by exchanging the promoter
- After each state is attracted with 50%, cells in a 'bad' attractor cannot grow, cells in a good attractor can grow, so that good attractors are selected?
NO!; the process occurs without (or before) the cell division process

Novel Mechanism of Spontaneous Adaptation (without the use of signal transduction) should exist!

- Growth-Induced-Attractor-Selection (Furusawa kk)
- Basic Logic

$$dx_i/dt = f(x_i) - S(\{x_j\})x_i + \eta(t)$$

$f \rightarrow$ Synthesis $S \rightarrow$ dilution due to cell growth

$\eta \rightarrow$ noise

Active state : both f and S are large

deterministic part \gg noise

Poor state : both f and S are small

deterministic part \sim noise

Switch from Poor state to Active state by noise

Selection before reproduction

General logic in a system with growth and fluctuation

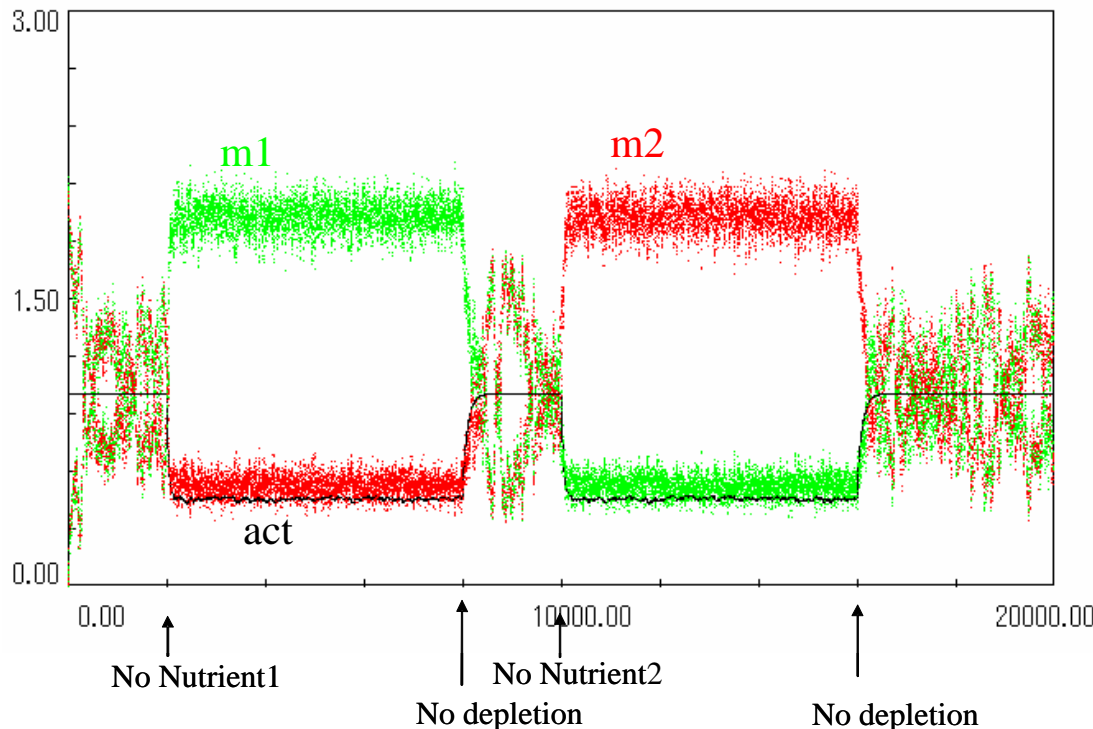
The mechanism for adaptive response by attractor selection

$$\frac{d}{dt}m1 = \frac{syn(act)}{1+m2^2} - deg(act) \times m1 + \eta_1$$

$$\frac{d}{dt}m2 = \frac{syn(act)}{1+m1^2} - deg(act) \times m2 + \eta_2$$

$$syn(act) = \frac{6act}{2+act}; deg(act) = act;$$

$$\frac{d}{dt}act = \frac{pro}{((\frac{Nut_thread_1}{m1+Nutrient1})^{n_1} + 1) \times ((\frac{Nut_thread_2}{m2+Nutrient2})^{n_2} + 1)} - cons \times act$$



Adaptive Response of the genetic network to a environmental change



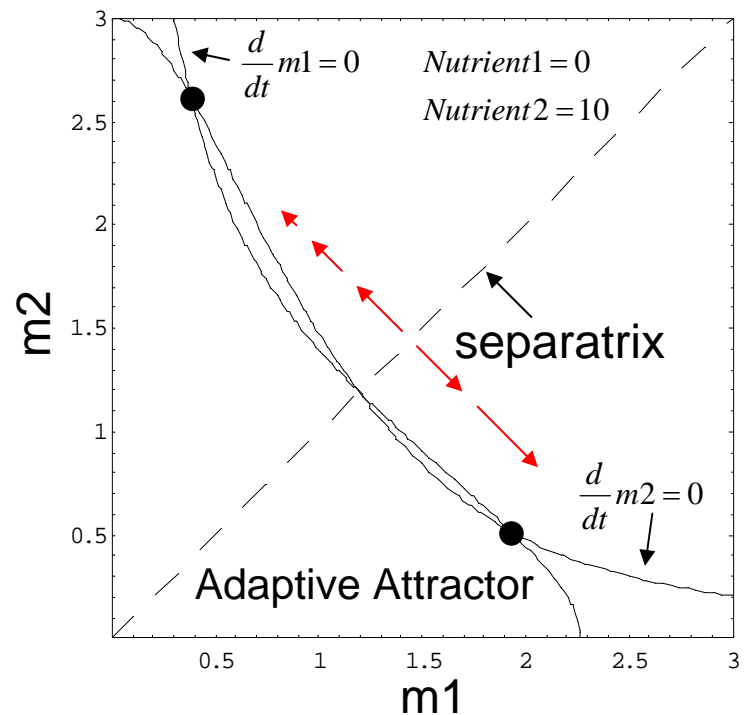
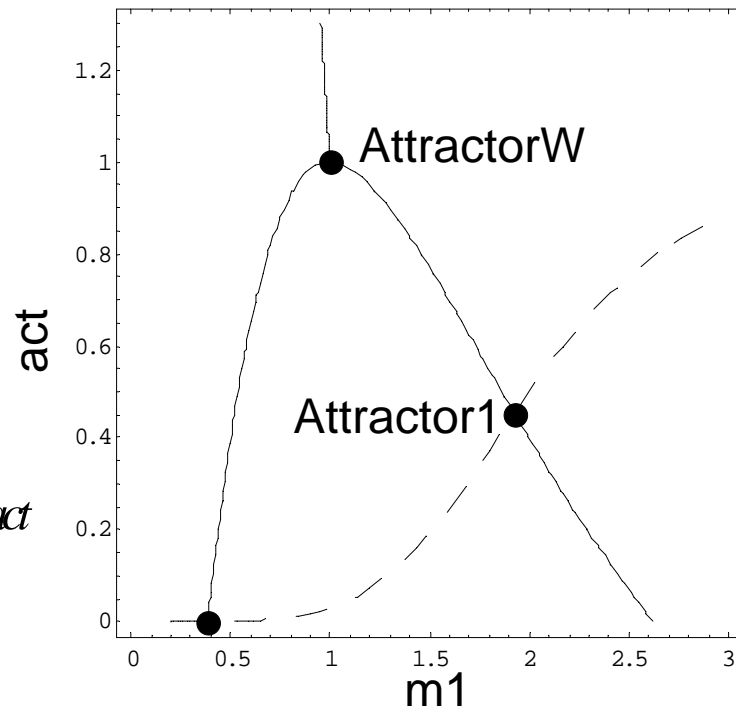
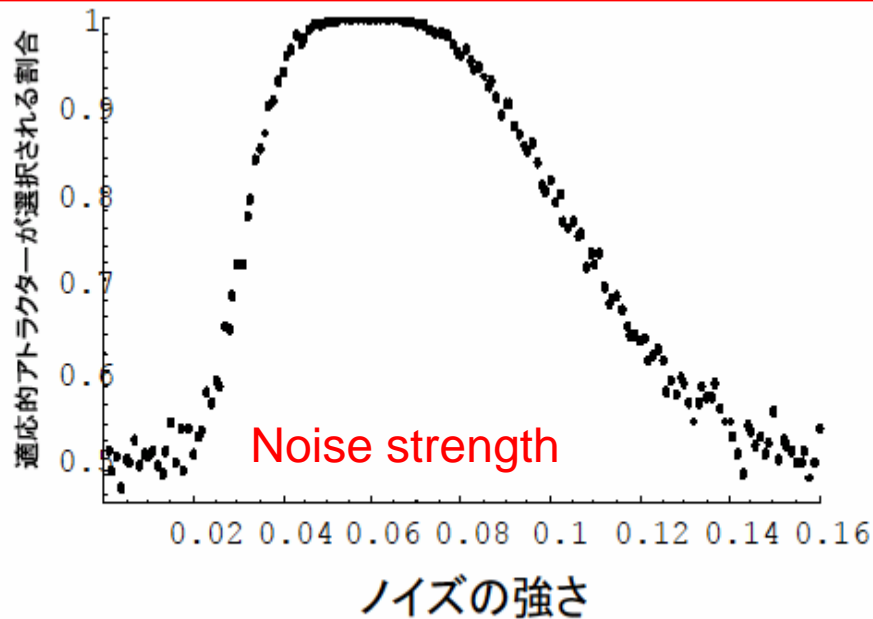
$$\frac{d}{dt} m1 = \frac{\text{syn}(\text{act})}{1 + m2^2} - \text{deg}(\text{act}) \times m1 + \eta_1$$

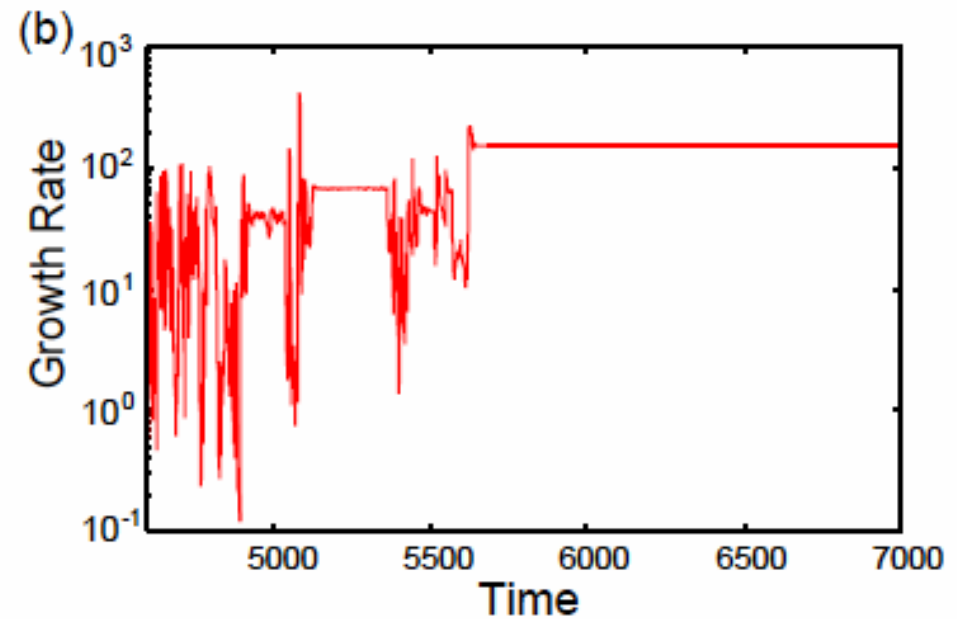
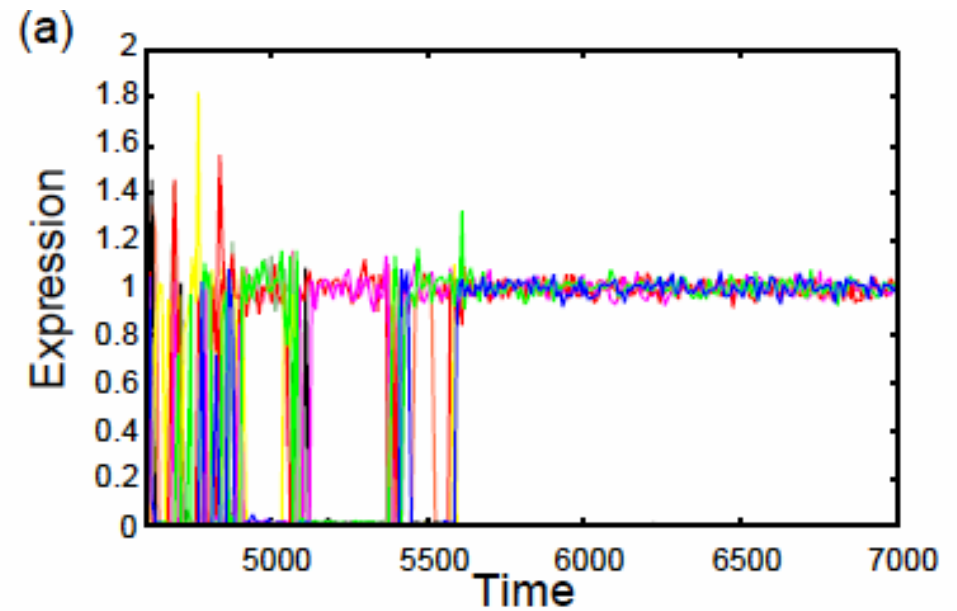
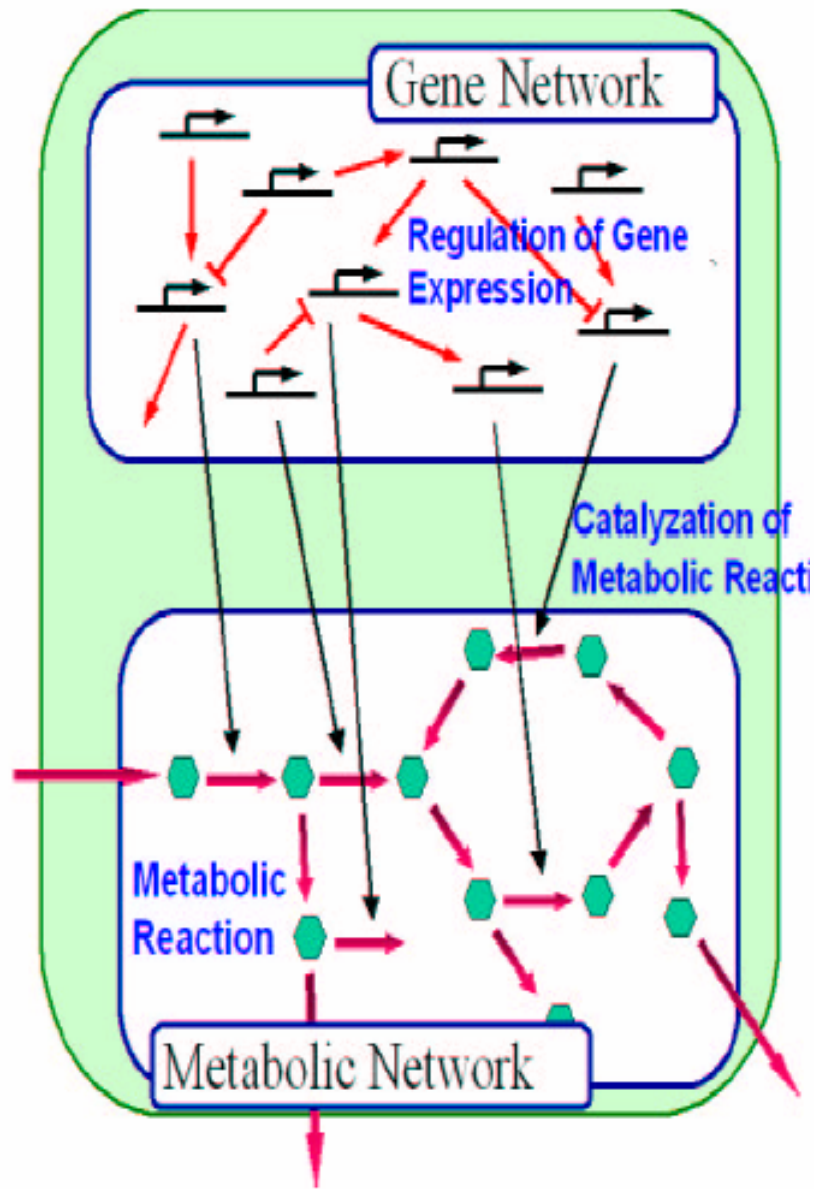
$$\frac{d}{dt} m2 = \frac{\text{syn}(\text{act})}{1 + m1^2} - \text{deg}(\text{act}) \times m2 + \eta_2$$

$$\text{syn}(\text{act}) = \frac{6\text{act}}{2 + \text{act}}; \text{deg}(\text{act}) = \text{act};$$

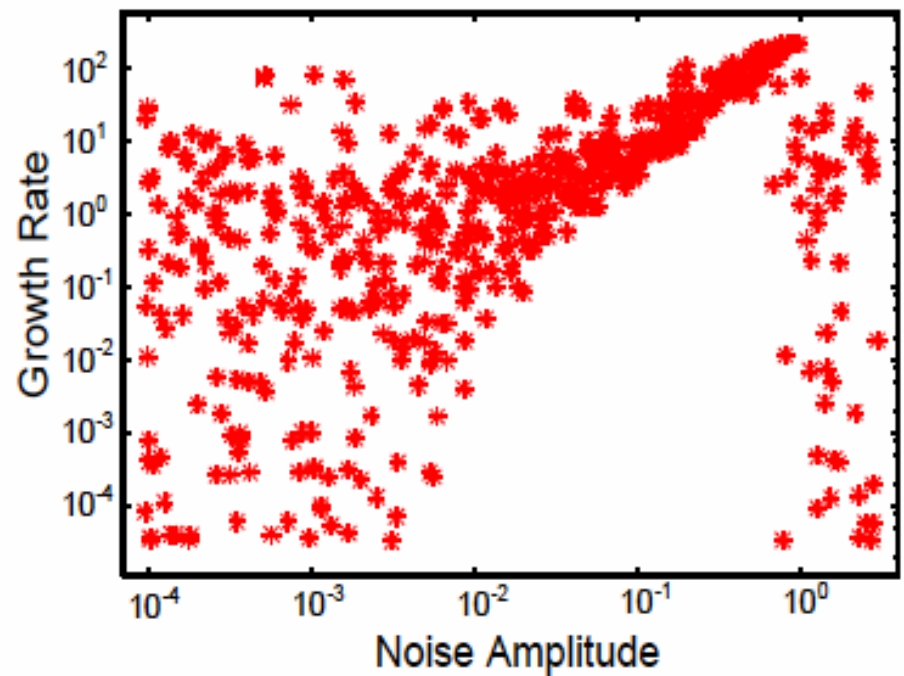
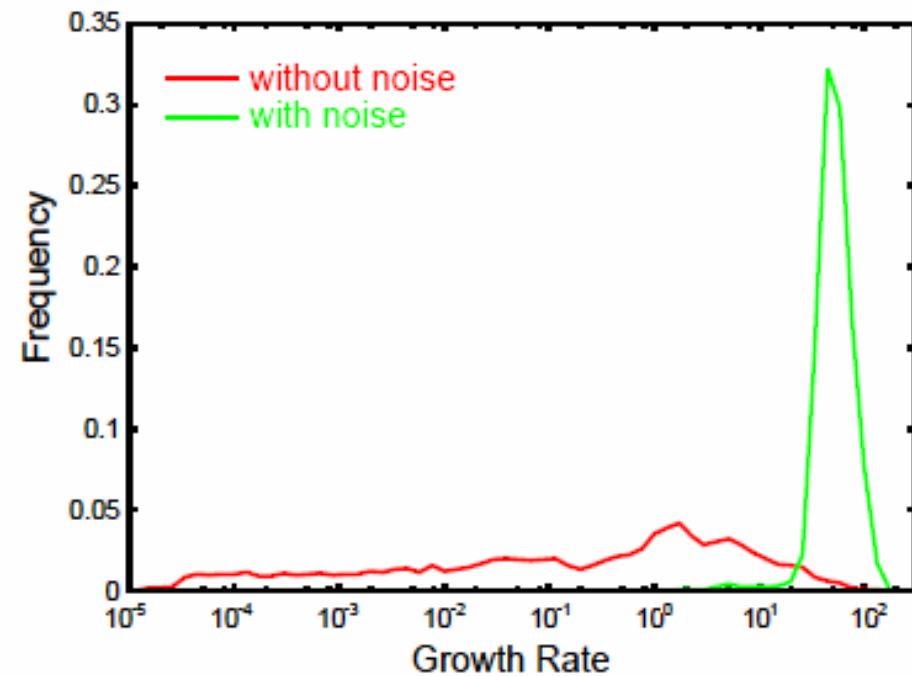
$$\frac{d}{dt} \text{act} = \frac{\text{pro}}{\left(\left(\frac{\text{Nut_thread}_1}{m1 + \text{Nutrient1}}\right)^{n_1} + 1\right) \times \left(\left(\frac{\text{Nut_thread}_2}{m2 + \text{Nutrient2}}\right)^{n_2} + 1\right)} - \text{cons} \times \text{act}$$

Fraction that adaptive attractor is selected



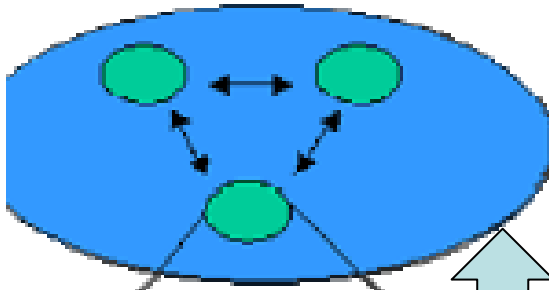


Gene network -> a huge number of attractors coexist with different growth speeds



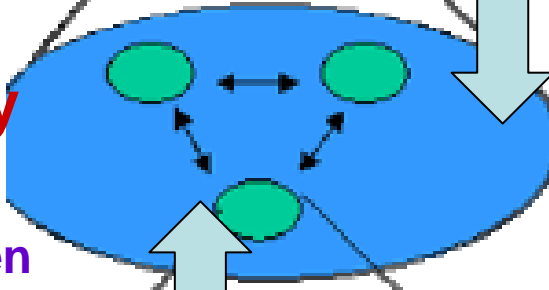
Spontaneous selection of optimal growth states
General in a system with noise and growth

Ecosystem



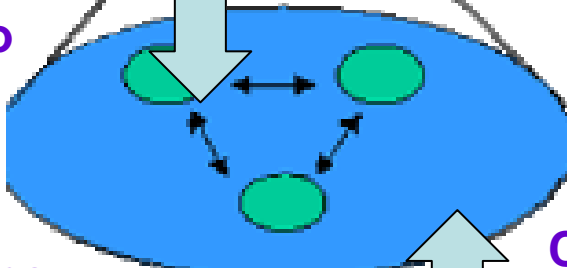
Phenotypic Plasticity vs Symbiosis
Or Ecological diversification

Multicellularity



Consistency between
Multicellular development
and cell reproduction

Cell



Evolutionary relationship on
Robustness and Fluctuation

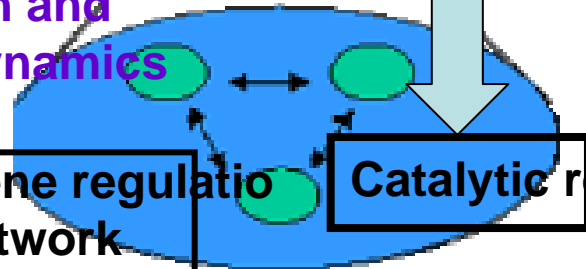
Genotype



Phenotype

Adaptation as
a result of consistency
between cell growth and
gene expression dynamics

Consistency between Cell reproduction
and molecule replication



**Gene regulation
network**

Catalytic reaction network

Molecule

Summary

Consistency Principle for Biology

- replication of molecules and cells : **Universal Laws**
(-- replication of cells and cell ensembles)
- adaptation of internal cellular state and growth
- genetic and phenotypic changes
(+speciation)
- Biological relevance of phenotype fluctuations?
 - **Phenotypic Fluctuation \propto Evolution Speed**
 - **Relation between**
(isogenic)phenotype fluctuation vs
phenotype variation by mutation
- Robustness to mutation and to developmental noise are linked
- Growth system → general adaptation by noise
- consequence of steady growth system

UNDERSTANDING
COMPLEX SYSTEMS

Springer:
COMPLEXITY

Kunihiko Kaneko

**Life:
An Introduction
to Complex
Systems
Biology**

 Springer

Collaborators

Chikara Furusawa

Katsuhiko Sato

experiment

Tetsuya Yomo

Yochiro Ito

Akiko Kashiwagi

Most papers (biology,
Dynamical systems)

Available at

<http://chaos.c.u-tokyo.ac.jp>

ERATO Complex Systems Biology Project

(2006, August)

Evolution of gene regulation network for more complex function:

Choice of complex dynamical systems to give gene expression pattern for segmentation

Found Two basic strategies to generate stripes

→ use of generic dynamics such as oscillation

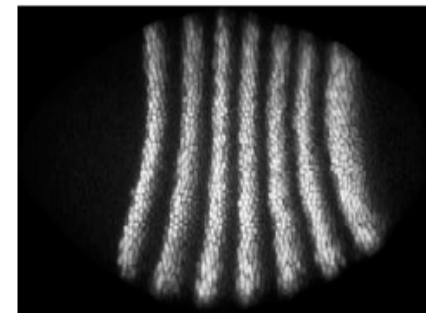
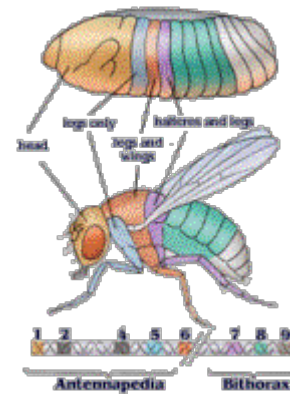
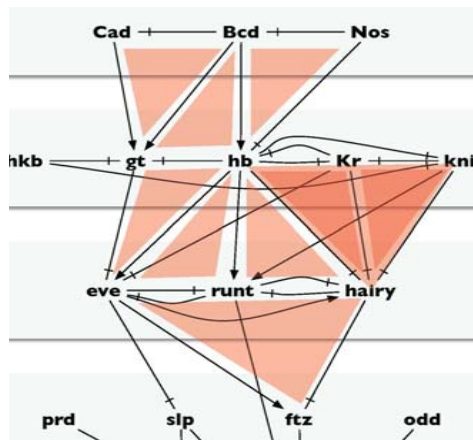
→ genetic control by logical (on/off) operations

(pioneered ; **Salzar-Ciudad, Newman, Sole, EvoDev2001**)

Network evolution of body plans

Fujimoto, Ishihara, KK (PLoS One 2008)

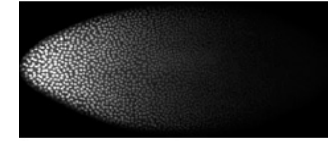
Also talk tomorrow by Fujimoto(>>4.4C1)



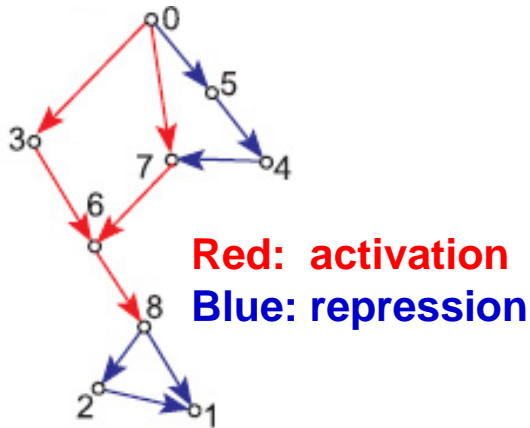
Even-skipped at the end of cell cycle 14

Method: Calculating development

- Take Gene regulation networks with activation and repression
- These genes are located spatially and chemicals diffuse (reaction+diffusion)



Becoid,
Drosophila

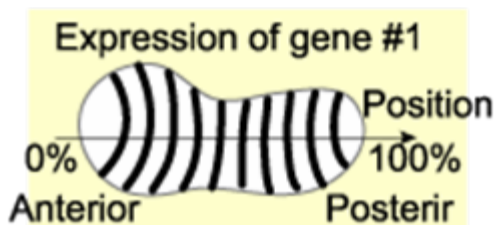


- Development under external environment as input (spatial gradient imposed)

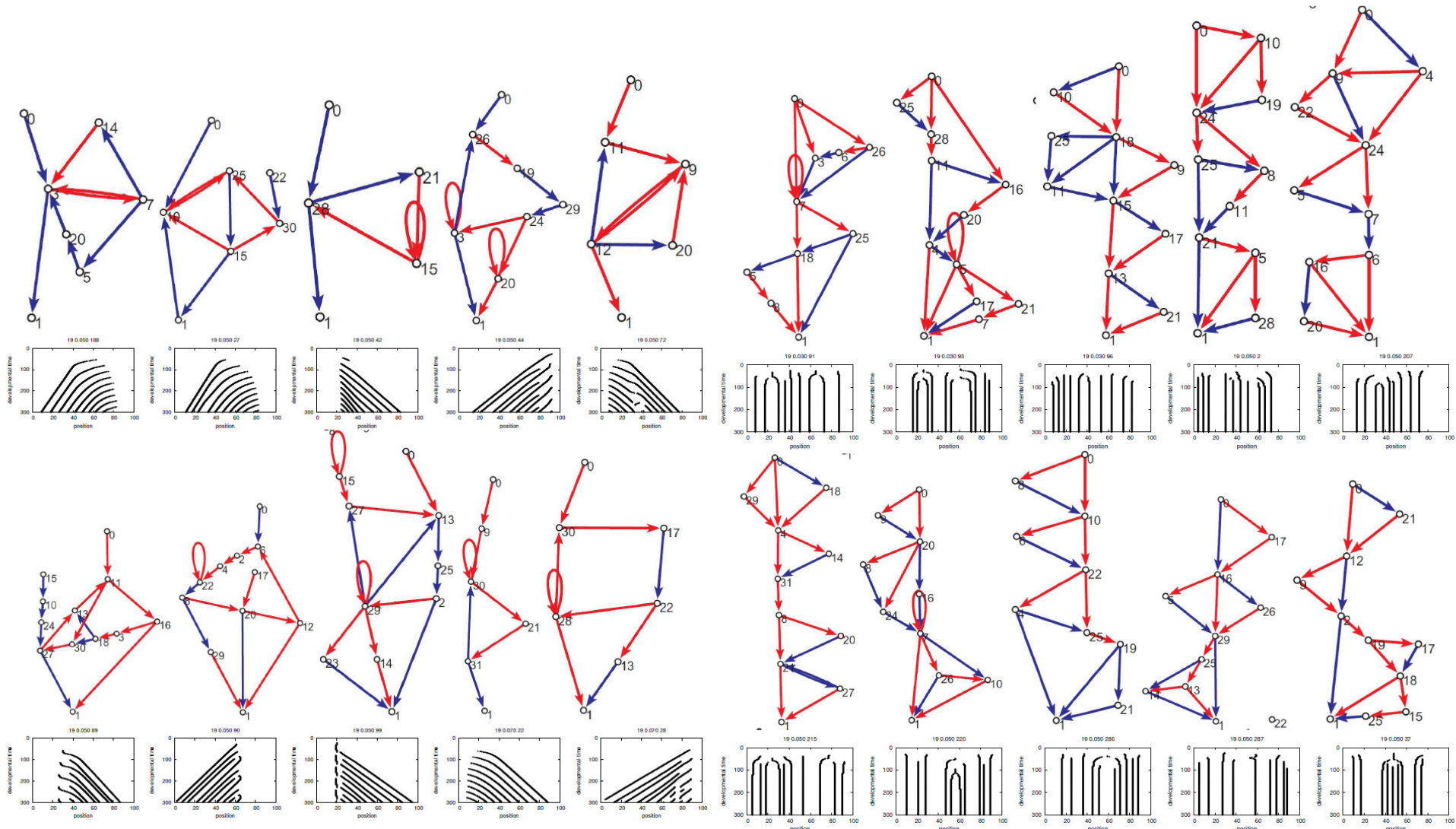
$$\frac{\partial Y}{\partial t} = -Y + f_Y(X, K_{xy}) + D_y \frac{\partial^2 Y}{\partial l^2}$$

- Gene #0 is distributed with spatial gradient.
- Reaction-diffusion equation for each gene expression.

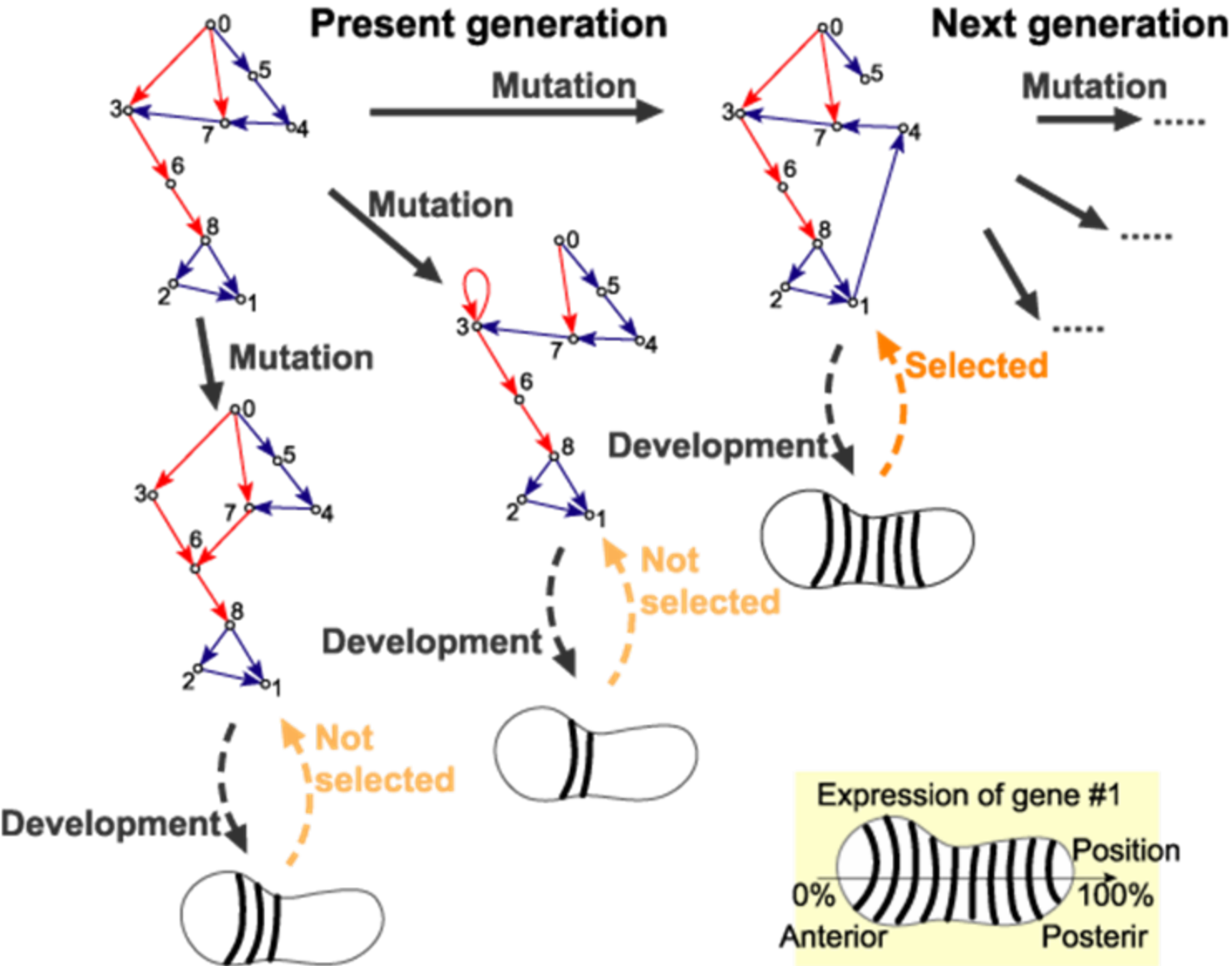
development



Strategy: Numerical evolution of gene regulatory networks to form stripe pattern.



Method: Numerical evolution

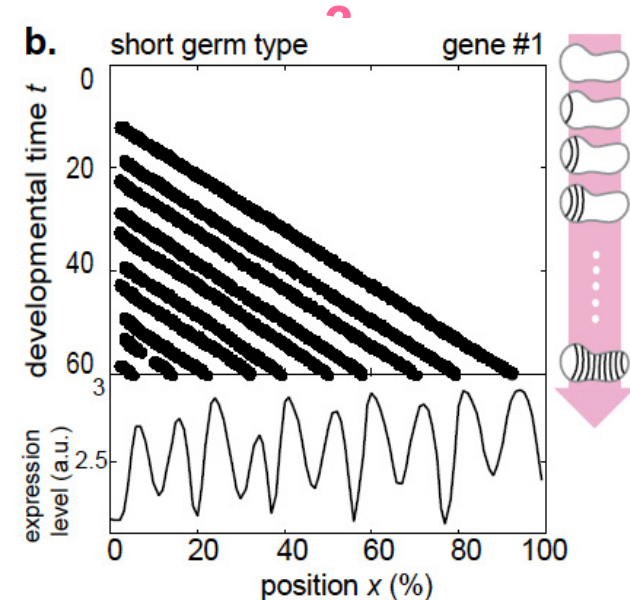
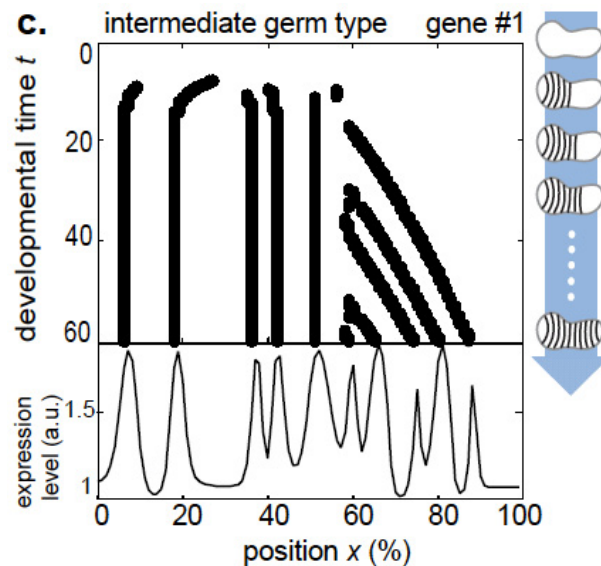
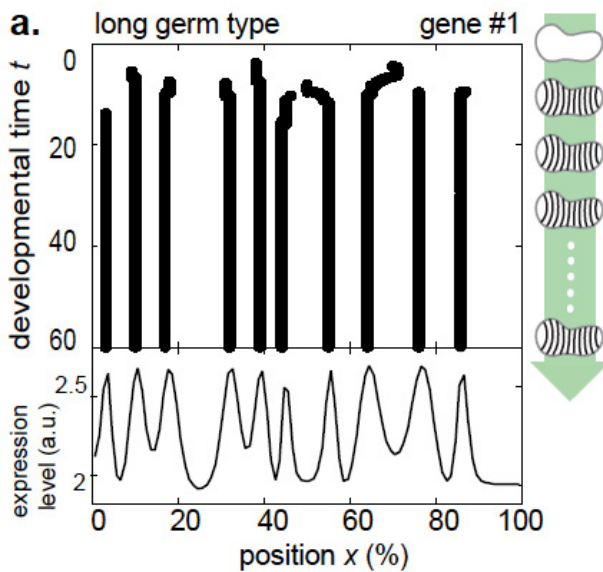


Development dynamics over >1000 evolved networks are classified **just into 3 modes**

**Long germ mode:
simultaneous**

**Intermediate germ
mode: combinatorial**

**Short germ mode:
sequential**



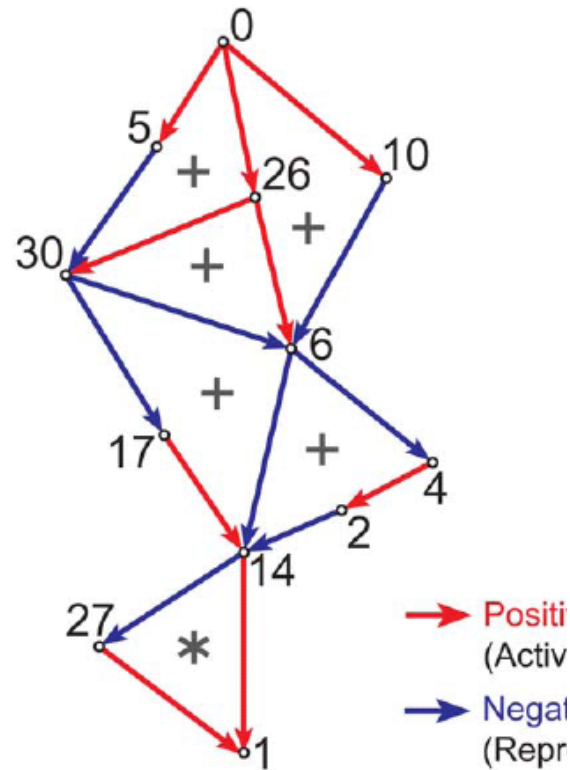
*** Simultaneous generation**
Combination of on/off regulations
by fixed expression dynamics

Sequential Generation
Use of oscillatory
gene expression

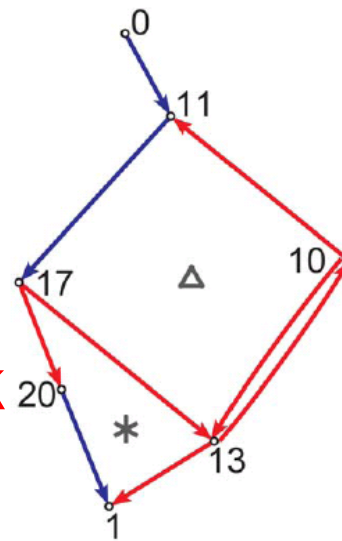
Difference in (core) network structure

Long-germ uses feed forward loop (FFL) dominantly

A. Long germ mode

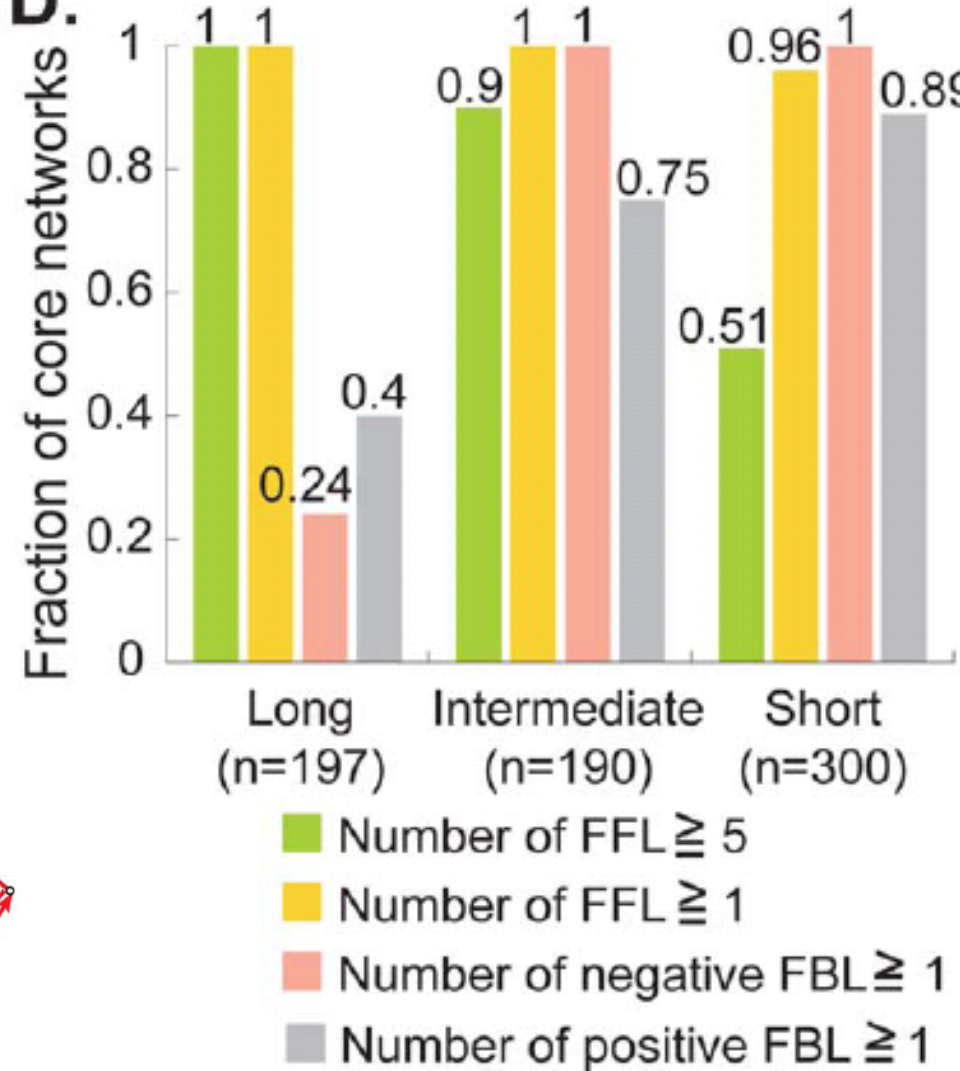


B. Short germ mode



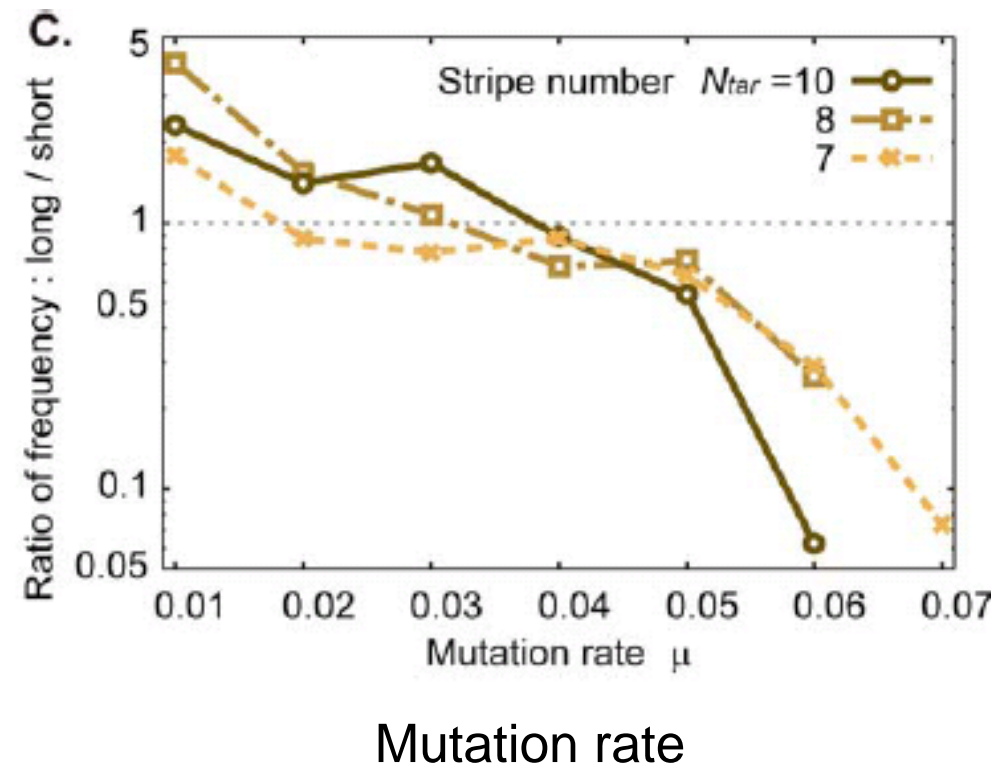
Short-germ uses mainly feed-back loop (FBL)

D.

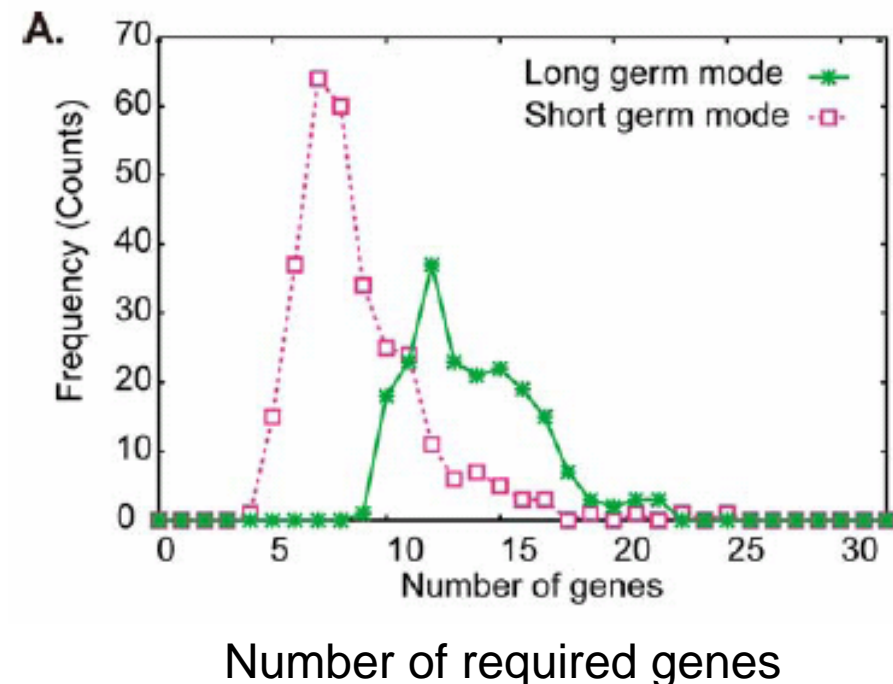


Short-germ mode has higher robustness to mutation to network, as the number of involved genes is fewer

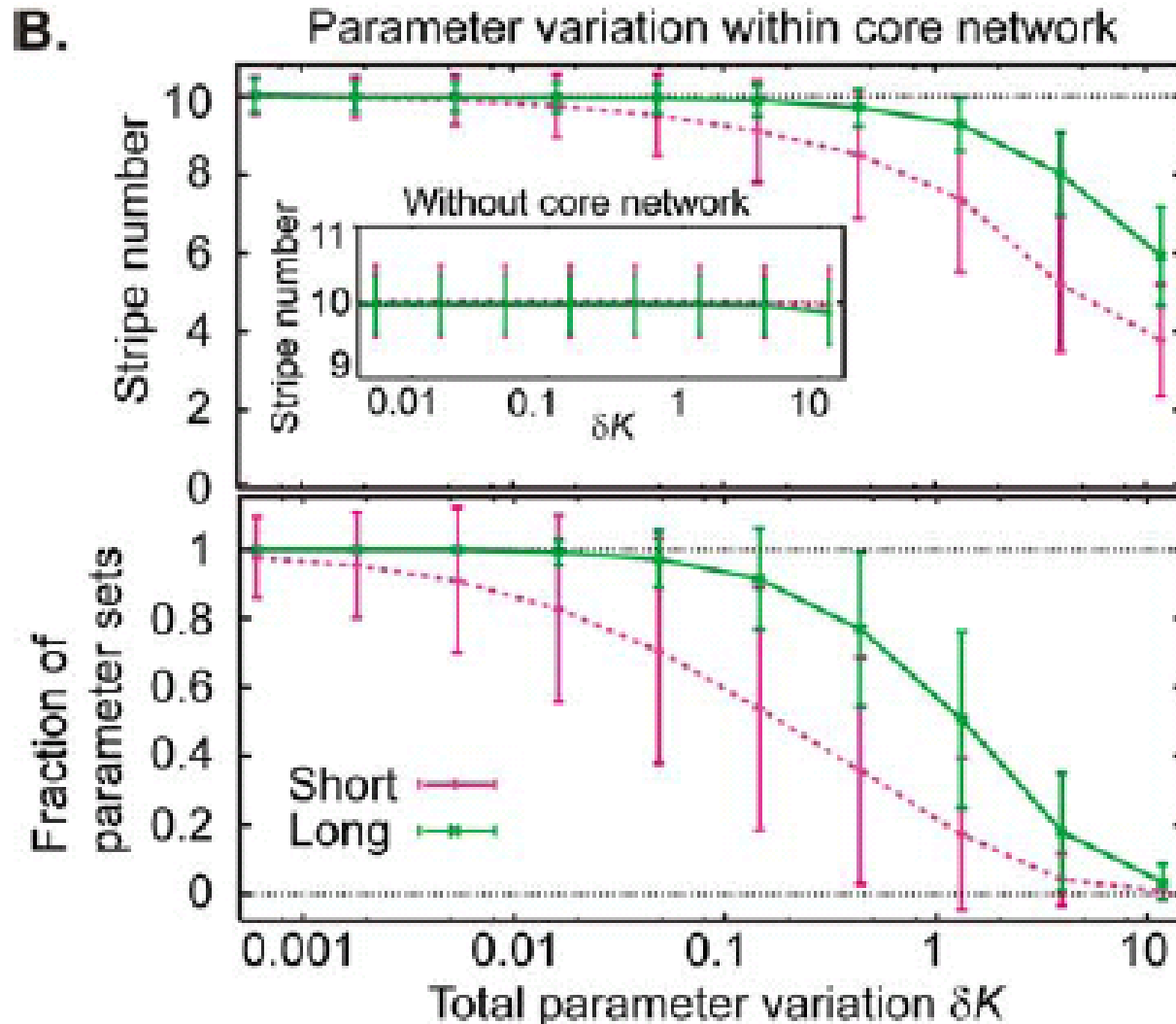
Ratio of Long to Short



Distribution of the number of required genes



Remarkably, however, Long Germ Mode development has **high robustness against changes in the parameters** in the gene expression dynamics



Summary

1. We classified networks according to **sequential** or **simultaneous** stripe formation.
2. They are characterized by network modules, **FBL** and **FFL**.
3. Compared them with observed **short** and **long** germ segmentation in arthropod.
4. Correspondences between numerical and real evolution suggest that the diverse segmentation is an inevitable property of evolving networks.

Segmentation mode	Pattern formation	Network module	Spatial Hierarchy	Knockout response	Development	Mutation rate
Short	sequential	FBL	No need	simple	Slower	Higher
Intermediate	combinatorial	FBL + FFL	?	variety		
Long	simultaneous	FFLs	necessary	variety	Faster	Lower